

TECHNICAL RESEARCH REPORT

Data Structures for Dynamic Queries: An Analytical and Experimental Evaluation

by V. Jain and B. Shneiderman

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**Data Structures for Dynamic Queries:
An Analytical and Experimental Evaluation**

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Abstract

Dynamic Queries is a querying technique for doing range search on multi-key data sets. It is a direct manipulation mechanism where the query is formulated using graphical widgets and the results are displayed graphically preferably within 100 milliseconds.

This paper evaluates four data structures, the multilist, the grid file, k-d tree and the quad tree used to organize data in high speed storage for dynamic queries. The effect of factors like size, distribution and dimensionality of data on the storage overhead and the speed of search is explored. Analytical models for estimating the storage and the search overheads are presented, and verified to be correct by empirical data. Results indicate that multilists are suitable for small (few thousand points) data sets irrespective of the data distribution. For large data sets the grid files are excellent for uniformly distributed data, and trees are good for skewed data distributions. There was no significant difference in performance between the tree structures.



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Abstract

Dynamic Queries is a querying technique for doing range search on multi-key data sets. It is a direct manipulation mechanism where the query is formulated using graphical widgets and the results are displayed graphically preferably within 100 milliseconds.

This paper evaluates four data structures, the multilist, the grid file, k-d tree and the quad tree used to organize data in high speed storage for dynamic queries. The effect of factors like size, distribution and dimensionality of data on the storage overhead and the speed of search is explored. Analytical models for estimating the storage and the search overheads are presented, and verified to be correct by empirical data. Results indicate that multilists are suitable for small (few thousand points) data sets irrespective of the data distribution. For large data sets the grid files are excellent for uniformly distributed data, and trees are good for skewed data distributions. There was no significant difference in performance between the tree structures.

1 Introduction

Most users of database systems must learn a querying language which they use to select and retrieve information. A query language is a special purpose language for constructing queries to retrieve information from a database of information stored in the computer [18].

Dynamic queries [1] is a novel way to explore information. This mechanism is well suited for multi-key data sets where the results of the search fit completely on a single screen. Figure 1 shows an application of dynamic queries in searching a real estate database. The query is formulated using widgets such as buttons and sliders, one widget being used for every key. A study [23] was conducted which compared dynamic queries (DQ) to a natural language system known

as "Q & A" and a traditional paper listing sorted by several fields. There was a statistically significant difference in the performance of the DQ interface compared to the other two interfaces. The DQ interface enabled users to perform faster and was rated higher than the other two in the terms of user satisfaction. The DQ interface was very useful in spotting trends and exceptions to trends as compared to the other two interfaces.

One of the important features of a DQ interface is the immediate display of the results of the query. In fact, users should be able to perform tens of queries in a span of a few seconds so that the mechanism remains dynamic. Using larger data sets slows down the mechanism so that there is a noticeable time interval (greater than 300 milliseconds) between the movement of sliders and the display of results.

The speed of DQ depends mainly on how the query is computed and the results displayed. The speed of display depends mainly on the graphic capabilities of the machine used. Even though the query computation depends to a great extent on the hardware of the machine used, it can be optimized to a great extent by using suitable data structures.

In this paper data structures for the high speed storage are examined. We assumed that the data sets remains frozen i.e. there are no insertions, deletions or updates. The time taken to load the data into the high speed storage memory i.e. the preprocessing time is ignored as it is done only once. Only simple rectangular queries are considered i.e. queries will be a simple conjunct of the ranges specified by the sliders.

2 Multi Attribute Range Search Methods

The problem of range search on multi attribute data sets can be defined as:

For a given multi-attribute data set, and a query which specifies a range for each attribute, find all records whose attributes lie in the given ranges.

The cost functions of various data structures are provided where N is the number of records, k is the number of attributes and F is the number of records found.

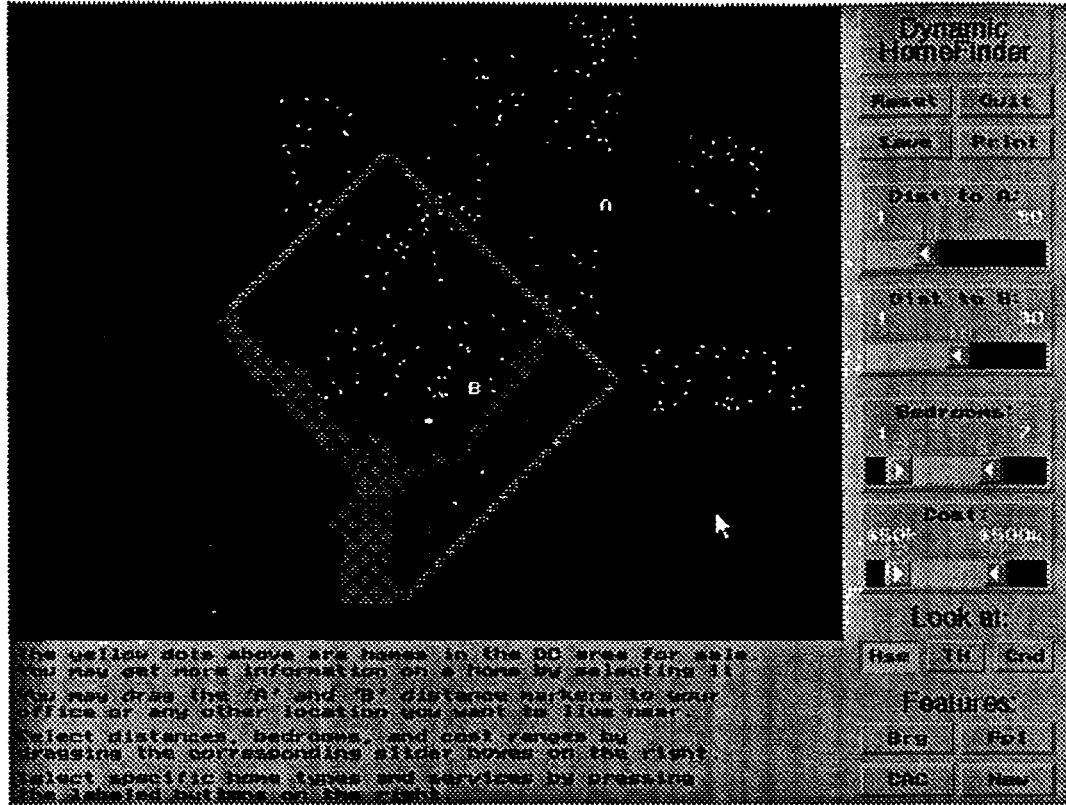


Figure 1: The Dynamic Home Finder

- $S(N, k)$ is the cost of storage required by the data structure.
- $Q(N, k)$ is the search time or query cost.

Figure 2 shows cost functions for structures that are suitable for rectangular queries. For the quad tree N_1 is the number of nodes in the tree. Further details about these data structures can be obtained from the references. Many other complex structures exist, but they are mainly of theoretical interest only because of their high storage overhead. It can be seen that range trees and k-ranges have relatively high storage overheads and are thus eliminated from consideration.

3 Data Structures

We assume the following characteristics of dynamic queries. The parameters of search are specified using sliders with one slider being used for each dimension. There are a limited number of positions the dragbox of a slider can take. This results in the ranges getting broken into discrete intervals. If every slider is assumed to break a range into G intervals, and if the data set has D dimensions then the search space can be split into G^D buckets. A bucket is the smallest unit of search and it is not possible to differentiate between points in a bucket. During search all or none of the data points of a bucket get included in the solution set. It may happen that

Data Structure	Storage Cost $S(N, k)$	Search Cost $Q(N, k)$
Sequential List	$O(Nk)$	$\mathcal{O}(Nk)$
Multilist	$O(Nk)$	$O(Nk)$
Cells	$O(Nk)$	$O(2^k F)$
k-d Tree	$O(Nk)$	$O(N^{1-1/k} + F)$
Quad Tree	$O(Nk)$	$O(N_1^{1-1/k} + F)$
Range Tree	$O(N \log^{k-1} N)$	$O(\log^k N + F)$
k-Ranges	$O(N^{2k-1})$	$O(k \log N + F)$

Figure 2: Storage and Search time overheads for various data structures

in certain data distributions some buckets are empty. Unlike the case in bucket methods for storage on disks, there is no limit on the number of points in a bucket when the high speed storage is used.

Four data structures are described in this section. The data points are stored in a simple array. It is assumed that points belonging to the same bucket will be stored consecutively. The data structures will be used to maintain an index on the array so that the search time is reduced. To maintain these indices, memory overhead is incurred which needs to be kept low. These structures can be classified in two categories i.e. bucket and non-bucket methods. In bucket methods an index is maintained on buckets and in non-bucket methods it is maintained on data points. The linked array which is a non-bucket method is described first. Later the bucket methods are described.

3.1 Linked Array

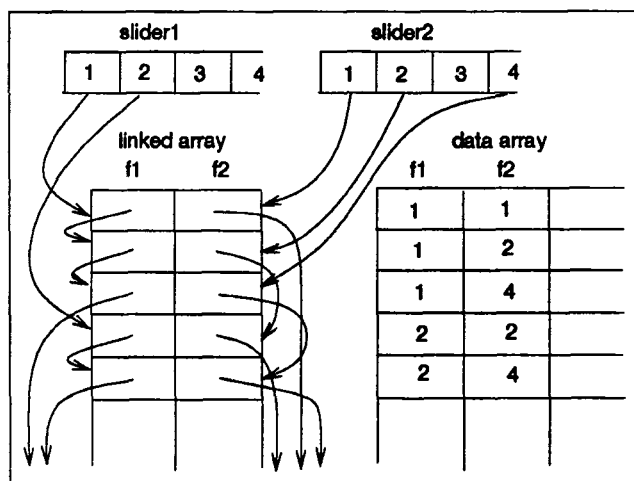


Figure 3: Linked Array used to index the Data Array

Figure 3 shows a part of the linked array when the data is two dimensional (i.e. $D = 2$). Also shown in the figure is a data array. The data array is an array which holds the data points. With every interval in the slider range is associated a linked list. Every point in the data set will lie in one and only one linked list of every slider. Also with every record is associated a flag (not shown in the figure). This flag keeps count of the number of fields of the record which satisfy the region of interest. When this count becomes equal to the number of dimensions then the record is displayed.

3.2 Grid Array

Figure 4 shows a part of the grid array used to index the data array for the two dimensional case. This is a bucket method and a bucket is essentially a pair of index numbers or pointers which point to the first and last record in the data array that belong to the bucket. These buckets form a part of the D dimensional search space. Therefore, to index them a D dimensional array is used.

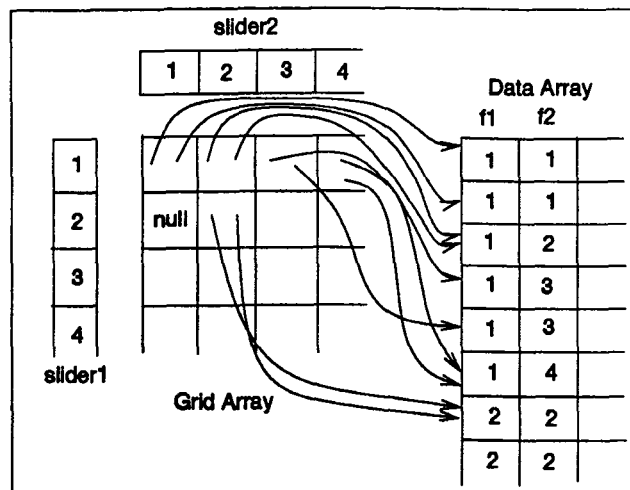


Figure 4: Grid Array used to index the Data Array

3.3 k-d Tree

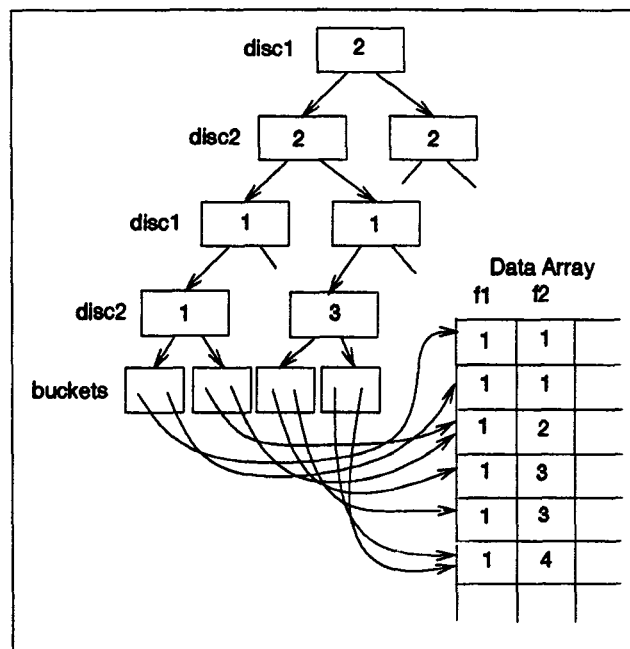


Figure 5: k-d Tree used to index the Data Array

Figure 5 shows a part of a k-d tree and the data array associated with it. In k-d trees, the concept of the buckets is again the same as the grid array. For our optimized k-d tree not all nodes at the same level in the tree have the same discriminator key. Nor are all the leaves at the same level. Therefore, in each node, besides the discriminator key value, the type of the discriminator key and a flag (not shown in the figure) which indicates the type of children (node or leaf) is also stored. This helps in reducing tree size when the number of non-empty buckets is small. It is possible that after optimization some leaves may move so that they are no longer at the level they were in the non-optimized tree. In such cases an additional check needs to be done to ensure that the bucket reached falls in the region of interest. A flag

(not shown in the figure) in the leaves indicates whether this check needs to be done.

3.4 Quad Tree

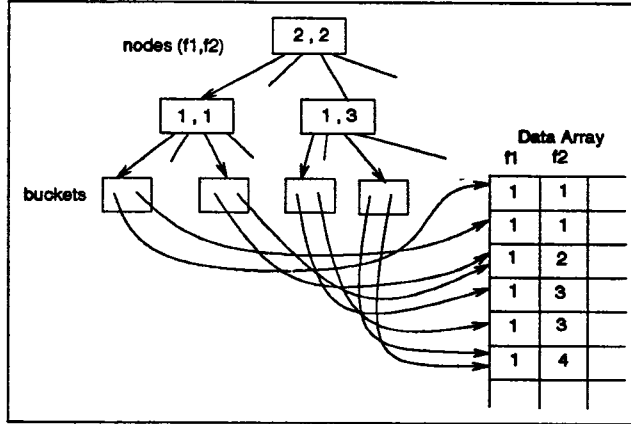


Figure 6: Quad Tree used to index the Data Array

Just as k-d trees could be used to index the buckets, quad trees can also be used to index the buckets as shown in Figure 6. Each node has D discriminator keys and 2^D pointers for the children. Just as in the case of a k-d tree, the children of a non-leaf node may be a mix of leaves and (non-leaf) nodes which is determined by a flag. One bit is required to maintain this information about each child. It is assumed that D is at most 5, hence the number of children is at most 32 and one word (32 bits or 4 bytes) suffices to store leaf/non-leaf information for all the children of a node. In some cases, after optimization, some leaves may move, (as in the k-d tree) and a check may be required to ensure correctness which is indicated by a flag.

4 Analytical Model

We analyze the storage and search overheads of data structures used for dynamic queries in this section. Storage overhead refers to the additional storage requirements for the data structure used. Search overhead is the number of operations required to compute the query result when the slider is moved. These two metrics will be used throughout this section to evaluate the data structures for dynamic queries. Search overhead will depend on how large the space being searched is. At any given moment the sliders define something called the *region of interest*, which is the portion of the search space being displayed. Every movement of a slider is a query which increases or decreases the region of interest. It is assumed that at any time only one dragbox of a slider will move in steps of one discrete interval. As a result of this move, points have to be removed or added to the display. In the case of the search overhead, it is assumed that the case where the region of interest is increasing will apply as a general case. For the worst case the increment in the region of interest should be the greatest. This happens when $D-1$ sliders have their left and right dragboxes in the extreme left

and right respectively. In this case with every move of the D^{th} slider G^{D-1} buckets are added to the region of interest. The effectiveness of a method will be studied with respect to factors such as the distribution, dimensionality (D) and size (N) of the data sets.

4.1 Comparing Bucket Methods

In this section a comparison of bucket methods is presented. Only the number of non-empty buckets will be considered in the analysis. The number of tuples does not effect the performance in any way. As mentioned earlier, two performance metrics used in the analysis are the storage overhead for the index on buckets and the worst case search time.

The following symbols will be used (i is the dimensionality):

- N : Number of points.
- D : Number of dimensions.
- G : Number of intervals in each slider range.
- No_i : Nodes in the structure.
- B_i : Non-empty buckets (leaves) in the structure.
- Nv_i : Nodes (non-leaf) visited (worst case).
- Bv_i : Non-empty buckets (leaves) visited (worst case).

The storage overhead is the cost of maintaining an index on the data points. In computing the storage overheads, it is assumed that each integer is 4 bytes, each character is 1 byte and each pointer is 4 bytes. If the number of dimensions is i , then the following holds true:

Grid Array: In grid arrays, 2 integer indices (first and last) are maintained for each bucket, irrespective of data distribution. So, 8 bytes are required for each bucket. Therefore, Total storage overhead = $8G^i$ bytes.

k-d Tree: In k-d trees, each non-leaf node has an integer discriminator key (4 bytes), a character discriminator key type (1 byte), a character flag for type of children (1 byte) and two pointers for left and right children (4 bytes each), resulting in a total of 14 bytes. Each leaf (non-empty bucket) has 2 integer indices (4 bytes each) and a character flag (1 byte), resulting in a total of 9 bytes. Therefore, Total storage overhead = $14No_i + 9B_i$ bytes.

Quad Tree: In quad trees, each non-leaf node has 2^i pointers for children of the node (4 bytes each), i integer discriminator keys (4 bytes each) and one flag for maintaining types of children (4 bytes), resulting in a total of $4(2^i + i + 1)$ bytes. Each leaf (non-empty bucket) requires 9 bytes as in the case of k-d trees. Therefore, Total storage overhead = $4(2^i + i + 1)No_i + 9B_i$ bytes.

The following assumptions have been made in calculating the search time overhead. i is used to indicate that the terms are for i dimensional case.

- For every non-empty bucket visited it is assumed that one operation is done to report that the bucket is non-empty.

- For the grid array one operation is required to visit a bucket and if it is non-empty then another operation is performed.
- For the k-d tree every non-leaf node visited has to be put into the stack and then later retrieved from the stack. This requires 2 operations. In processing every node two comparisons have to be made. This makes it a total of 4 operations for every non-leaf node visited. In visiting leaves, 2 operations will always be required: 1 operation for reporting that the bucket is non-empty (as discussed earlier) and 1 operation to get to the leaf. In some cases, because of the optimizations on the tree that were discussed earlier, an additional check is required to ensure that the bucket reached is the correct one. This may require up to $2i$ operations.
- For the quad tree every non-leaf node visited has to be put into the stack and later retrieved from the stack. This requires 2 operations. $2i$ comparisons are required to determine which children of the node to search. 2 operations are required for checking the flags to determine the type of children. So, in all $2i+4$ operations are done for every non-leaf node visited. In visiting leaves, 2 operations will always be required: 1 operation for reporting that the bucket is non-empty (as discussed earlier) and one operation to get to the leaf. As in the case of k-d trees, an additional check may be required to ensure correctness of the leaf reached which requires $2i$ operations.
- In the worst case, for both k-d tree and quad tree, it is assumed that the number of nodes visited, when the data is i dimensional is No_{i-1} . This is because in the worst case $i-1$ sliders do not restrict the search in any way. The slider restricting the search has only one of its discrete intervals to be searched for. It is like taking a slice of thickness 1 from the i dimensional search space.

4.1.1 Uniform Data Distribution

In this subsection we present the storage overheads and search time requirements for the case when the data distribution is uniform. An important factor effecting these performance metrics is the percentage of buckets which are non-empty. Two extreme cases were considered in this subsection, when all the buckets are non-empty and when only 25% of the buckets are non-empty. We briefly state the important results here. Detailed analysis for deriving these results is presented in [11].

Figures 9 and 10 show how the storage and search overheads vary as the fraction of non-empty buckets changes for uniformly distributed data. The values used were, $G = 16$ and $D = 4$. Figures 7 and 8 show the overheads for the case of uniformly distributed data. These results indicate that, the grid array is a significantly better structure to use when data is uniformly distributed and most buckets are non-empty. It has a lower memory and search time overhead than both the tree structures. However as the number of empty buckets rises the difference in the memory overhead

Data Structure	Storage Cost	Search Cost
Grid Array	$8G^D$	$2G^{D-1}$
k-d Tree	$23G^D$	$6G^{D-1}$
Quad Tree	$4(2^D + D + 1)\frac{G^D}{2^{D-1}} + 9G^D$	$(2D + 4)\frac{G^{D-1}}{2^{D-1-1}} + 2G^{D-1}$

Figure 7: Storage and Search time overheads for Uniformly Distributed Data (100% buckets non-empty)

Data Structure	Storage Cost	Search Cost
Grid Array	$8G^D$	$5\frac{G^{D-1}}{4}$
k-d Tree	$\frac{23G^D}{4}$	$5\frac{G^{D-1}}{2}$
Quad Tree	$4(2^D + D + 1)\frac{G^D}{2^{D-1}} + 9\frac{G^D}{4}$	$(2D + 4)\frac{G^{D-1}}{2^{D-1-1}} + \frac{G^{D-1}}{2}$

Figure 8: Storage and Search time overheads for Uniformly Distributed Data (25% buckets non-empty)

reduces and the trees get better. When comparing the search overheads of the structures for the case where most buckets are non-empty the quad tree has a lower search overhead. The dimensionality of the data only increases the differences with the differences in performance becoming greater as dimensionality rises.

4.1.2 Skewed Data Distribution

In this subsection, the performance of data structures is examined when the data distribution is skewed. Two cases are examined, when all the non-empty buckets are only along the diagonal of the search space and the case where all the non-empty buckets are within a distance of $G/4$ from the diagonal. As in the case of uniformly distributed data the detailed analysis is presented in [11].

Figures 11 and 12 show the overheads for the case of skewed distributions. These results indicate that, there is a significant difference between the performance of trees and the grid array with the trees being superior. This is reflected both in memory and search overheads. For the case where non-empty buckets lie only along the diagonal of the search space the difference in the trees and the grid is phenomenal. In the second case also the trees are significantly better. Amongst the trees it can be said that the k-d tree has a marginally lower memory overhead and a marginally higher search overhead than the quad tree. As in the case of uniformly distributed data, higher dimensionality of data makes the differences more pronounced.

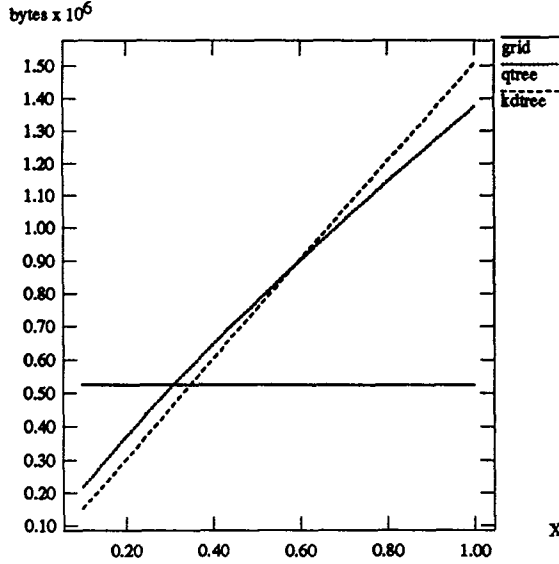


Figure 9: Memory overhead for Uniformly Distributed Data Vs. the fraction of non-empty buckets

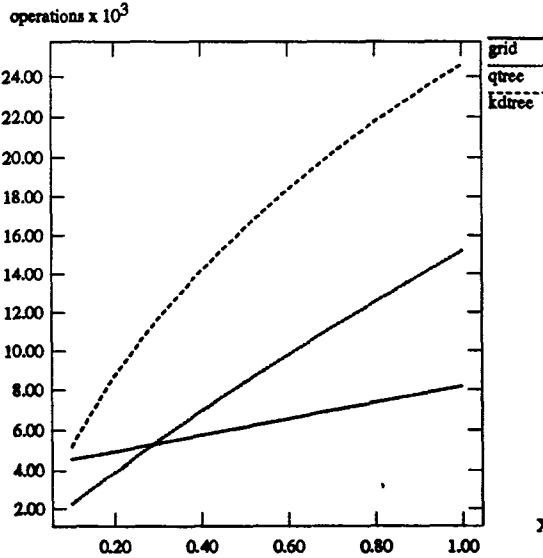


Figure 10: Search overhead for Uniformly Distributed Data Vs. the fraction of non-empty buckets

Data Structure	Storage Cost	Search Cost
Grid Array	$8G^D$	G^{D-1}
k-d Tree	$23G$	$4\log_2 G + 2D + 2$
Quad Tree	$4(2^D + D + 1)G + 9G$	$(2D + 4)\log_2 G + 2$

Figure 11: Storage and Search time overheads for Skewed Data Distribution (non-empty buckets along diagonal only)

Data Structure	Storage Cost	Search Cost
Grid Array	$8G^D$	$\frac{G^{D-1}}{4} + \frac{B_D}{G}$
k-d Tree	$23B_D$	$4B_{D-1} + (2D + 2)\frac{B_D}{G}$
Quad Tree	$4(2^D + D + 1)No_D + 9B_D$	$(2D + 4)No_{D-1} + 2\frac{B_D}{G}$

Figure 12: Storage and Search time overheads for Skewed Data Distribution (all non-empty buckets within a distance of $G/4$ of diagonal)

4.2 Bucket Vs Non-Bucket Methods

In bucket methods the number of points does not effect the search overhead if the number of points is sufficiently large to make most buckets non-empty. However when the number of points is small or the number of dimensions is low it may be better to use the linked array because its storage overhead is directly proportional to the number of points in the data set and the dimension of the data set.

- Every tuple of the linked array has to be kept on D lists. For this D additional pointers (4 bytes) are needed. In addition a flag (1 byte) is required (see section 3.1). Therefore, storage overhead is $(4D + 1)N$.
- Generally each linked list associated with a slider will have N/G tuples in it. Therefore, search overhead (worst case and average case) is $\frac{N}{G}$.

The linked array was compared to the grid array for uniform data distributions. Only the grid array was chosen because it has a superior performance compared to the trees for uniform distribution. With a value of $G = 16$ and $D = 4$, it was seen that the linked array performed much better as far as the search overhead is concerned. However the storage overhead for this structure gets very high.

The linked array was compared with the tree structures for the skewed distribution. The grid array was dropped from consideration here because trees perform better under skewed data distributions. In this case the performance of

the tree structures, specially the quad tree is much better both when storage overhead and search overheads are compared. One reason could be that in skewed distributions the bucket occupancy rises very steeply when compared to the uniform distributions.

5 Experimental Results

The analytical models of section 4 were verified by implementing the cases discussed. The implementation was done on a dedicated SUN 4/50 with 16 MB of memory and running SunOS. The memory overhead was calculated by counting the nodes and leaves for the bucket methods, and the number of points for the linked array. Clock time in microseconds was used to measure the speed of search instead of the number of operations as in section 4. The process switching overhead was ignored as the machine had negligible load.

5.1 Comparing Bucket Methods

The analytical models of subsection 4.1 were implemented and the results are presented in this subsection. In the calculation of memory overhead, only the extra memory required to maintain the index was considered. As mentioned before in calculating the search time, the time for display of records was ignored. The value of $G = 16$ was used in implementations.

5.1.1 Uniform Data Distribution

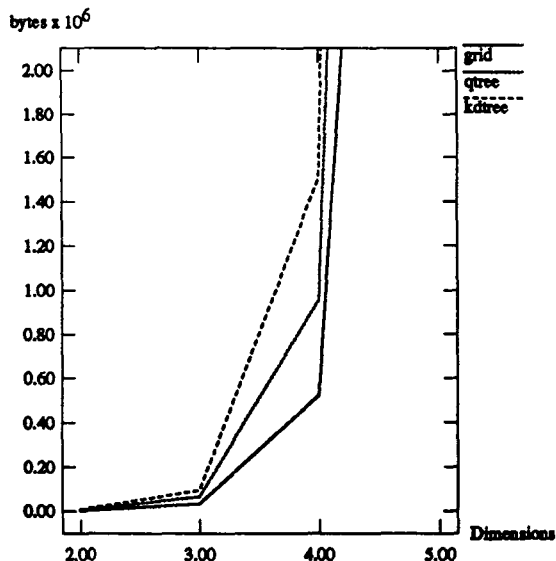


Figure 13: Memory overhead for Uniformly Distributed Data (100% buckets non-empty)

Figures 13 and 14 show the results of the memory and search time overhead respectively for the case where all buckets are

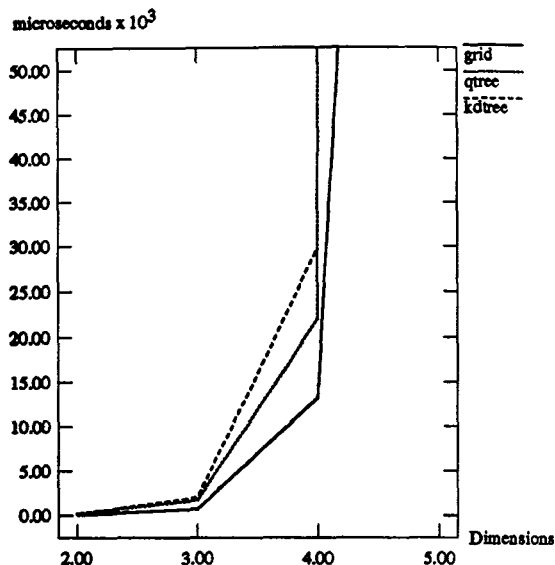


Figure 14: Search overhead for Uniformly Distributed Data (100% buckets non-empty)

non-empty. For this case the grid array is significantly better than the tree structures both in terms of memory overhead and search time overhead.

The case where 25% of the buckets are empty is shown in figures 15 and 16. The grid array is a significantly better structure when search time overhead is considered. However the k-d tree is marginally better when memory overhead is considered. All results in this subsubsection closely match previous analytical models.

5.1.2 Skewed Data Distribution

Figures 17 and 18 show the results of the memory and search time overhead respectively for the case where non-empty buckets are only along the diagonal. For this case both the k-d tree and the quad tree give a performance far superior to the grid array both for memory overhead and search time overhead. However there is no significant difference between the performance of trees.

When all points lie in buckets within a distance $G/4$ of the diagonal the tree structures turn out to be excellent performers compared to the grid array. This can be seen clearly in figures 19 and 20. However the difference between the tree structures themselves is not large. It should be noted that as in the previous cases the results of the implementations follow the analytical models closely.

5.2 Bucket Vs Non-Bucket Methods

In the calculation of memory overhead for linked array, only the extra memory required to maintain the linked list was considered. As mentioned before in calculating the search time, the time for display of records found was ignored. The

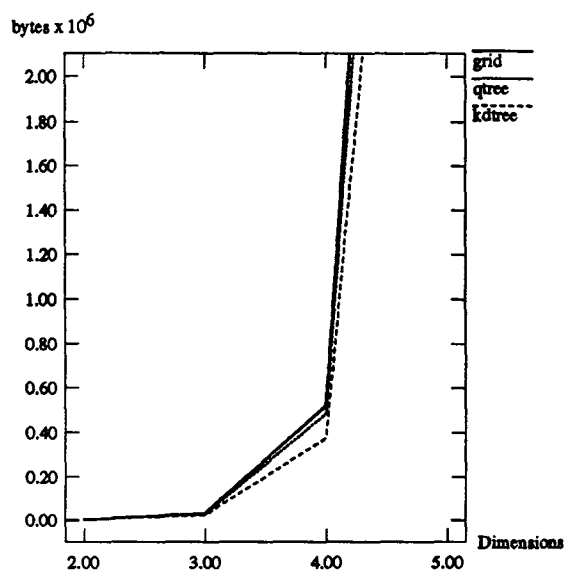


Figure 15: Memory overhead for Uniformly Distributed Data (25% buckets non-empty)

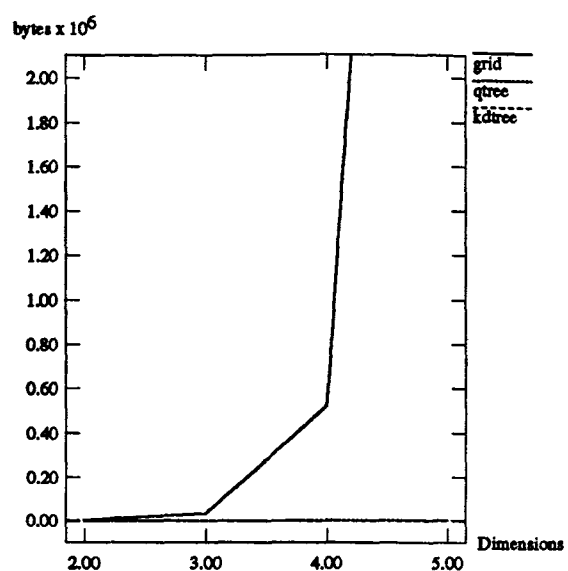


Figure 17: Memory overhead for Skewed Data Distribution (non-empty buckets along diagonal only)

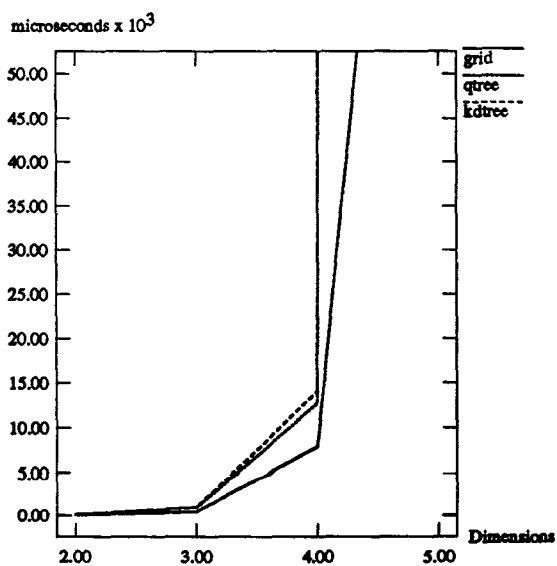


Figure 16: Search overhead for Uniformly Distributed Data (25% buckets non-empty)

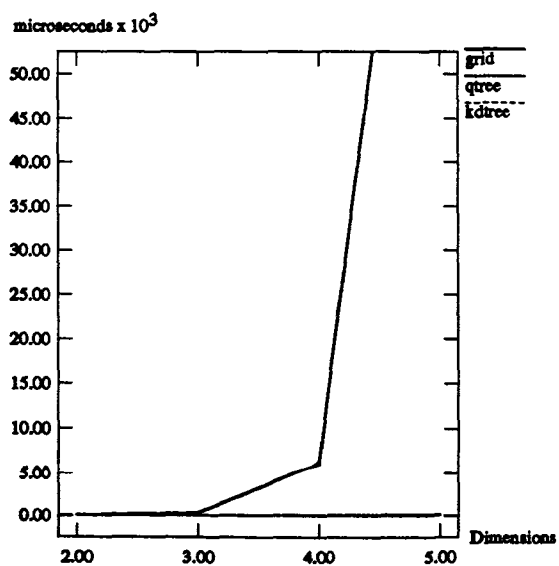


Figure 18: Search overhead for Skewed Data Distribution (non-empty buckets along diagonal only)

values of $G = 16$ and $D = 4$ were used in the implementations.

5.2.1 Uniform Data Distribution

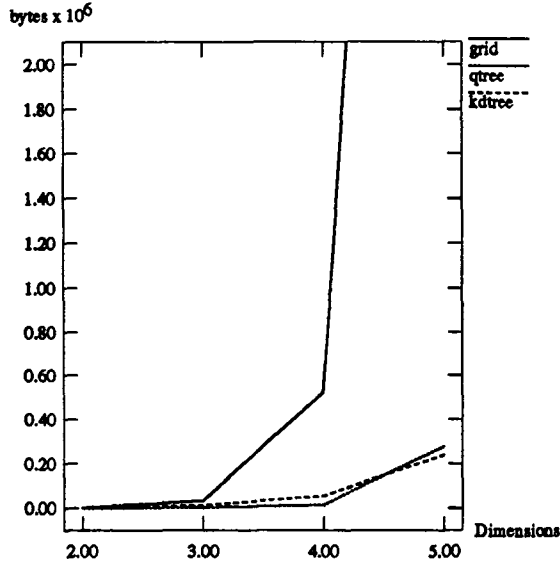


Figure 19: Memory overhead for Skewed Data Distribution (all non-empty buckets within a distance of $G/4$ of diagonal)

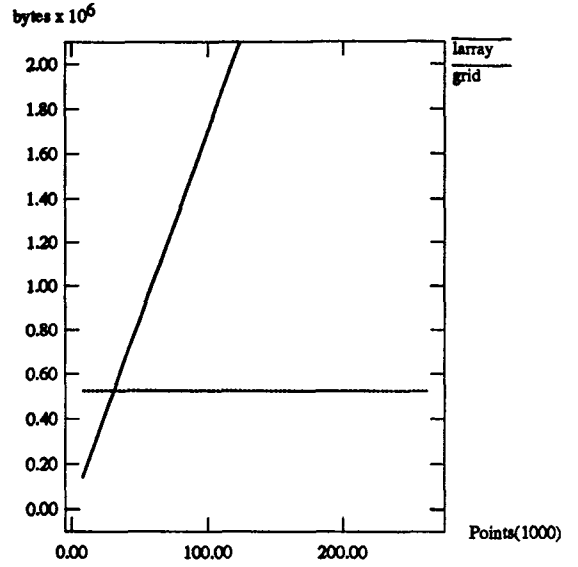


Figure 21: Memory overhead for Uniformly Distributed Data

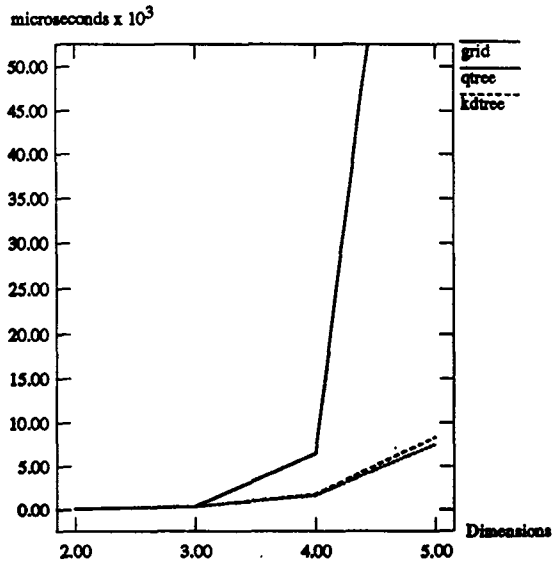


Figure 20: Search overhead for Skewed Data Distribution (all non-empty buckets within a distance of $G/4$ of diagonal)

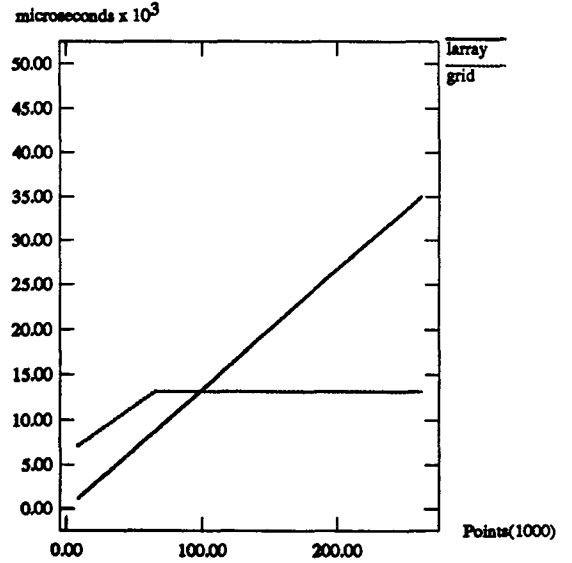


Figure 22: Search overhead for Uniformly Distributed Data

Figures 21 and 22 show the comparison between the linked array and the grid array. As mentioned before in subsection 5.2 only the grid array was chosen among bucket methods as it has the best performance for uniformly distributed data. As far as search time overhead is considered the linked array performed better than the grid for up to approximately 100,000 points. However the drawback is that the memory

overhead for this structure keeps increasing as the size of the data set increases unlike the case for the grid array where it remains a constant.

5.2.2 Skewed Data Distribution

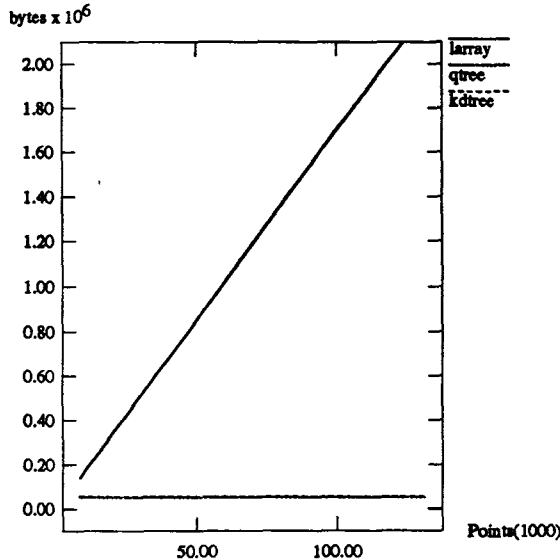


Figure 23: Memory overhead for Skewed Data Distribution (all non-empty buckets within a distance of $G/4$ of diagonal)

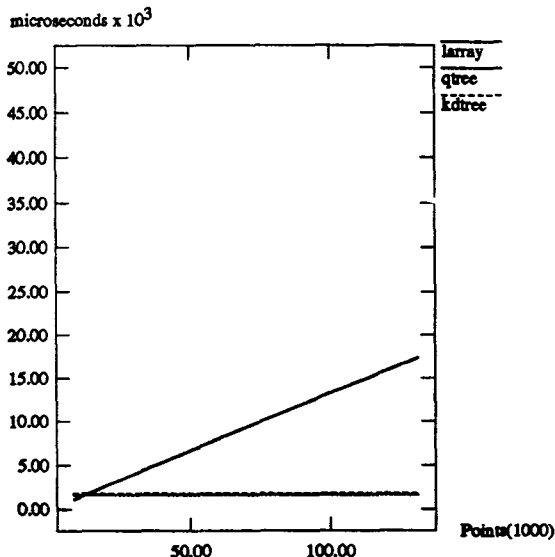


Figure 24: Search overhead for Skewed Data Distribution (all non-empty buckets within a distance of $G/4$ of diagonal)

Figures 23 and 24 show the comparison between the linked array and the tree structures for skewed distributions. As mentioned before in subsection 5.2 only the trees were chosen among bucket methods as they have significantly better performance for skewed data distribution. When compared

to the linked array the tree structures get significantly better than the linked array both in terms of search time and memory overhead. However when the number of tuples is small (about 10,000) it is better to use a linked array because of its simplicity.

6 Conclusions

6.1 Contributions

We have presented a way of analyzing data structures for dynamic query applications. The usefulness of analytical models was shown by empirical data. In almost all cases the empirical results confirmed the analytical models.

In the case of uniformly distributed data the linked array structure performed quite well but the drawback in this structure is that its memory overhead is very high and therefore it should be used only for small data sets. For larger data sets it is recommended that a grid array be used. The advantage in the grid array is that the memory overhead does not depend on the number of points in the data set but only on the number of buckets in the data set.

For skewed data distributions where most of the buckets are empty, the performance of tree structures, was much better than the grid array. Among tree structures the k-d tree used marginally less memory but had a marginally higher search overhead. Compared to the linked array again the trees were much better except for the cases where the number of data points were just a few thousand. However there is a temptation to use the linked array because of its simplicity. It is recommended that the tree structures be used for skewed data distributions if the number of points exceed a few thousand.

In cases where knowledge of the data distribution is lacking we recommend using the k-d tree as it is highly likely that the distribution is non-uniform. The k-d tree is also much easier to construct compared to the quad tree when the ranges of the sliders are not equal. It was noticed that the performance of a data structure does not change with the dimensionality of the data set. The only effect of increasing dimensions is that the number of buckets increases, which results in the differences in the performance becoming more pronounced.

The data structures discussed in this paper are practical and make it possible to implement dynamic queries on standard machines in common use without major special requirements. This is essential, specially because in addition to experts, novice users with inexpensive machines also find DQ very appealing.

6.2 Future Directions

The assumption that data sets are frozen could be dropped and the effect of updates on these data structures would be interesting. Another assumption about the nature of queries, where queries were assumed to be a simple conjunct of ranges

could be relaxed, opening up another area of investigation. The segregation of data into buckets can also lead to interesting methods for compression.

Using dynamic queries with very large data sets raises many interesting issues. It would be impossible to store all data in main memory and disk accesses become a necessity. It would be worth while to study applications where data is organized on disks. Approaching dynamic queries from the distributed databases point of view would be another solution for large data sets. Another approach to take is making dynamic queries run on parallel machines.

One of the reasons dynamic query applications are effective is because they present query results in a way to help users visualize the data set. Therefore effective ways of visualizing data, specially multi-dimensional data are important for the success of dynamic queries.

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References

- [1] C. Ahlberg, C. Williamson, and B. Shneiderman, "Dynamic Queries for Information Exploration: An Implementation and Evaluation", *Proc. CHI'92, ACM*, New York, 1992, pp. 619-626.
- [2] D.A. Beckley, M.W. Evans and V.K. Raman, "Multikey Retrieval from K-d Trees and Quad-Trees", *Proc. ACM SIGMOD International Conference on the Management of Data*, Austin, 1985, pp. 291-301.
- [3] J. L. Bentley, "Multidimensional Binary Search Trees Used for Associative Searching", *Communications of the ACM*, Vol. 18, No. 9, 1975, pp. 509-517.
- [4] J. L. Bentley and D. F. Stanat, "Analysis of Range Searches in Quad Trees", *Information Processing Letters*, Vol. 3, No. 6, 1975, pp. 170-173.
- [5] J. Bentley and J. Friedman, "Data Structures for Range Searching", *Computing Surveys*, Vol. 11, No. 4, December 1979, pp. 397-409.
- [6] J. Bentley and H. Maurer, "Efficient Worst-Case Data Structures for Range Searching", *Acta Informatica*, Vol. 13, No. 2, 1980, pp. 155-168.
- [7] C. Faloutsos and P. Bhagwat, "Declustering Using Fractals", *2nd International Conference on Parallel and Distributed Information Systems*, San Diego CA, 1993, pp. 18-25.
- [8] R. A. Finkel and J. L. Bentley, "Quad Trees, A Data Structure for Retrieval on Composite Keys", *Acta Informatica*, Vol. 4, 1974, pp. 1-9.
- [9] H. Garcia-Molina and K. Salem, "Main Memory Database Systems: An Overview", *IEEE Transactions on Knowledge and Data Engineering*, Vol. 4, No. 6, 1992, pp. 509-516.
- [10] A. Guttman, "R-Trees: A Dynamic Index Structure for Spatial Searching", *Proc. ACM SIGMOD Conference*, Boston, 1984, pp. 47-57.
- [11] V. Jain and B. Shneiderman, "Data Structures for Dynamic Queries: An Analytical and Experimental Evaluation", CfAR Technical Report, University of Maryland, College Park, No. CAR-TR-685, September 1993.
- [12] D. E. Knuth, "The Art of Computer Programming, Vol. 3: Sorting and Searching", Addison-Wesley, 1973.
- [13] D. T. Lee and C. K. Wong, "Worst-Case Analysis for Region and Partial Region Searches in Multidimensional Binary Search Trees and Balanced Quad Trees", *Acta Informatica*, Vol. 9, 1977, pp. 23-29.
- [14] D. Lomet, "A Review of Recent Work on Multi-attribute Access Methods", *SIGMOD RECORD*, Vol. 21, No. 3, September 1992, pp. 56-63.
- [15] V. Y. Lum, "Multi-attribute Retrieval with Combined Indexes", *Communications of the ACM*, Vol. 13, No. 11, 1970, pp. 660-665.
- [16] J. Nievergelt and H. Hinterberger, "The Grid File: An Adaptable, Symmetric Multikey File Structure", *ACM Transactions on Database Systems*, Vol. 9, No. 1, March 1984, pp. 38-71.
- [17] M. Regnier, "Analysis of Grid File Algorithms", *BIT*, Vol. 25, 1985, pp. 335-357.
- [18] P. Reisner, "Human Factors Studies of Database Query Languages: A Survey and Assessment", *Computing Surveys*, Vol. 13, No. 1, 1981, pp. 13-31.
- [19] H. Samet, "The Design and Analysis of Spatial Data Structures", Chapter 2, Addison Wesley 1989.
- [20] P. Scheuermann and M. Ouksel, "Multidimensional B-Trees for Associative Searching in Database Systems", *Information Systems*, Vol. 7, No. 2, 1982, pp. 123-137.
- [21] B. Shneiderman, "Direct Manipulation: A Step Beyond Programming Languages", *IEEE Computer*, Vol. 16, No. 8, August 1983, pp. 57-69.
- [22] B. Shneiderman, "Designing the User Interface: Strategies for effective Human-Computer Interaction", Second Edition, Chapter 5, Addison-Wesley 1992.
- [23] C. Williamson and B. Shneiderman, "The Dynamic Homefinder: Evaluating Dynamic Queries in a Real-Estate Information Exploration System", *Proc. ACM SIGIR Conference on Information Retrieval*, Copenhagen Denmark, 1992.

