Title of thesis: RESILIENCE OF NETWORKED INFRASTRUCTURE WITH EVOLVING COMPONENT CONDITIONS: A PAVEMENT NETWORK APPLICATION

Ali Asadabadi, Master of Science, 2016

Thesis directed by: Professor Elise Miller-Hooks, Department of Civil and Environmental Engineering

This thesis deals with quantifying the resilience of a network of pavements. Calculations were carried out by modeling network performance under a set of possible damage-meteorological scenarios with known probability of occurrence. Resilience evaluation was performed a priori while accounting for optimal preparedness decisions and additional response actions that can be taken under each of the scenarios. Unlike the common assumption that the pre-event condition of all system components is uniform, fixed, and pristine, component condition evolution was incorporated herein. For this purpose, the health of the individual system components immediately prior to hazard event impact, under all considered scenarios, was associated with a serviceability rating. This rating was projected to reflect both natural deterioration and any intermittent improvements due to maintenance. The scheme was demonstrated for a hypothetical case study involving Laguardia Airport. Results show that resilience can be impacted by the condition of the infrastructure elements, their natural deterioration processes, and prevailing maintenance plans. The findings imply that, in general, upper bound values are reported in ordinary resilience work, and that including evolving component conditions is of value.
RESILIENCE OF NETWORKED INFRASTRUCTURE WITH EVOLVING COMPONENT CONDITIONS: A PAVEMENT NETWORK APPLICATION

by

Ali Asadabadi

Thesis submitted to the Faculty of the Graduate School of the University of Maryland, College Park, in partial fulfillment of the requirements for the degree of Master of Science 2016

Advisory Committee:
Professor Elise Miller-Hooks, Chair
Professor Paul Schonfeld
Dr. Sandra Knight
Dedication

To my beloved parents, Mohamad Taghi and Soraya, and my dear siblings, Elham and Arash.
Acknowledgements

I would like to thank those who helped me getting this work done. First of all, I want to thank my advisor Dr. Elise Miller-Hooks, who constantly guided me through this learning journey and provided the support during my studies at University of Maryland. I want to thank my senior student Reza Faturechi for his help, mentoring and guidance as well as his invaluable body of research on which this work tries to expand. I also like to thank Dr. Eyal Levenberg for his central role in work that led to this thesis and his efforts in preparing the paper for ASCE journal. I am thankful to civil engineering faculty member Dr. Schonfeld whom I had the opportunity to learn a lot from and accepted to serve in my defense committee. I want to thanks Sandra Knight for her valuable help as a member of my defense committee. I want to thank my dear friend Azadeh for her support.
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Chapter 1: Introduction

Networked civil infrastructures, such as transportation, water, and energy systems, are essential to the functioning of any modern society, and therefore must be resilient. Numerous works have focused on the development and quantification of resilience metrics, and some have proposed normative models for such systems. Common to their definitions is a concept of system-level coping capacity under multi-component damage due to, for example: extreme meteorological conditions, geological hazards, and human-made events of an accidental or intentional nature. Damage to the system may also originate from less extraordinary events. In this context, resilience is generally conceived in terms of the system’s ability to absorb damage thus continuing to serve the intended purpose, and recover within an acceptable time and cost (e.g., Holling 1973; Haimes 2009; The White House 2015; National Infrastructure Advisory Council 2015).

An underlying and typically unstated assumption in treating resilience is that the pre-event condition of all system components is uniform, fixed, known, and pristine. This means that resilience evaluations are, in effect, specific to the pre-event condition assumed at the moment of analysis as if the damage events were imminent. In reality, at a given point in time, the level of ‘health’ across components is uneven, with some offering a reduced inherent ability to endure damage. That is, infrastructure component integrity evolves over time. Two main governing and competing factors determine infrastructure integrity: (i) Progressive condition deterioration under usual service as a result of the combined effects of physical and environmental loading (i.e.
“wear-and-tear” and aging), and (ii) Maintenance activities that aim for partial or complete condition renewal, or merely for slowing the natural deterioration rate (i.e., preventative). Based on a thorough review of the literature (Faturechi and Miller-Hooks 2015) which scanned over 200 articles, it appears that other than two works by Dehghani et al. (2013, 2014), no prior work on resilience or related performance measure computation has explicitly accounted for non-pristine integrity, timewise evolution, and subsequent unevenness in system component conditions. Dehghani et al. (2014) assessed expected network performance in terms of vehicle miles traveled and other devised vulnerability metrics over multiple randomly generated generic disruption scenarios involving link failures. Both papers discuss the need for condition-based vulnerability assessment as advocated herein, or more specifically, the need to incorporate each element’s condition in replicating link failure probabilities. Their application in (Dehghani et al., 2014) on a hypothetical example demonstrates that a range over network performance results from assuming different link probability failure distributions (i.e. all link failures are either uniform, beta or normal). Herein, this general idea of a need for condition-based assessment is furthered.

This work proposes and demonstrates a condition-based resilience quantification methodology that incorporates component-condition evolution in a systems-based analysis. Resilience calculations, which may include resilience enhancing preparedness and response actions, are carried out under a set of possible damage-meteorological scenarios with known probability of occurrence. Each scenario consists of hazard type identification, meteorological state, number of affected segments (damage extent), and damage severity in terms of required repair duration
and resources. The evaluation is performed \textit{a priori} while accounting for optimal response actions that can be taken under each of the scenarios; preparedness actions that improve resilience are also optimized. To account for condition evolution, the health or integrity level of the individual system components immediately prior to hazard event impact (under all considered scenarios) is associated with a serviceability rating. This rating is projected to reflect both usual deterioration and policy-guided improvements due to maintenance. Impacts from generated damage-meteorological events are made to depend on the pre-impact serviceability ratings, exemplifying the added vulnerability of deteriorated components. The quantification scheme also captures the increased damage extent, extra repair costs, and longer repair times due to pre-event non-pristine conditions.

Hereafter, pavement condition and its expression through serviceability is first described. Then, an existing concept of resilience is restated and subsequently expanded to incorporate component serviceability rating. The formulation is applied next to an airport case study to demonstrate the value and effect of including natural deterioration and maintenance policies in resilience quantification. Lastly, gained insights and main conclusions of the study are listed and discussed. It is important to note that the applicability of the concepts and general methodology presented herein transcend this pavements application, generally applying to a system of components whose conditions differ, deteriorate over time and are influenced by maintenance and/or replacement actions. Specific models of deterioration/serviceability, maintenance or renewal planning, or system resilience as throughput or other will differ based on the use, but the framework is designed to be generally applicable.
Moreover, it accounts for the system impacts of multiple link-based maintenance and resilience enhancements.
Chapter 2: Pavement Condition Evolution

2.1 The Serviceability Concept

Without repair actions, pavements progressively deteriorate with time. The decline is directly associated with structural or physical damage involving distress modes, such as: rutting, cracking, longitudinal roughness, and raveling. It therefore represents a timewise diminishment in coping capacity against damage events of operational (e.g., overloading), natural (e.g. flooding), or other causes. The degradation pattern is case-specific as it depends upon the pavement design, as-built mechanical properties of the different layers, traffic intensity, and prevailing climatic conditions.

The concept of serviceability is often employed in the pavement arena for quantifying infrastructure condition. The idea was introduced and developed during the 1960’s in conjunction with the AASHO road experiment (Carey and Irick 1960). In this experiment, different full-scale road sections were intensively trafficked for a period of two years by trucks of known weight, axle configurations, and travel speed. At the same time, the evolution of surface distress was closely monitored and recorded. A serviceability rating in the range of 5 (=pristine) to 0 (=worst possible), was adopted to quantify the condition of each road section from a user and structural perspective. Initially, the rating was based upon a subjective visual score given by a group of experts examining the ride surface (Present Serviceability Rating, PSR); it was later correlated with objectively measurable damage such as density of cracked or patched zones, longitudinal roughness, etc (Present Serviceability Index, PSI). In the AASHO
road test, a power-law expression was found adequate for all pavement types to describe the evolution of serviceability as a function of traffic loadings:

\[
S = S_i - (S_i - S_f) \left( \frac{W}{\rho} \right)^\beta, \tag{2.1}
\]

where \( S \) denotes the current serviceability rating, \( S_i \) is the initial serviceability rating prevailing immediately after construction, \( S_f \) is the final or unacceptable serviceability rating, and \( W \) is the cumulative number of equivalent vehicle passes applied to the section up to point for which \( S \) is calculated. In effect, if the traffic intensity is timewise uniform, \( W \) may be seen as equivalent to age. The parameters \( \rho \) and \( \beta \) are regression constants that embody the experimental setup, such as pavement layering arrangement and mechanical properties, prevailing environmental conditions, and loading characteristics of passing vehicles. By substituting \( S = S_f \) it may be noticed that \( \rho \) equals the value of \( W \) at failure. Graphically, the deterioration pattern (i.e., the shape of \( S \) vs. \( W \) curve) depends upon the value of \( \beta \); for \( \beta = 1 \) the curve is an oblique line, for \( \beta > 1 \) the curve is concave, while for \( \beta < 1 \) it is convex.

The AASHO deterioration function is well recognized and still widely utilized in engineering practice. At the same time it is deemed restrictive, incapable of correctly matching observed long-term pavement behavior, mainly because its curvature never reverses as needed (Fwa 1990). This shortcoming was later rectified by considering a slightly different equation capable of producing an S-shaped curve (Garcia-Diaz and Riggins 1984):
\[ S = S_i - \frac{S_i - S_f}{\exp((\tau / t)^n)}, \]  

(2.2)

wherein \( t \) is the time since construction or time elapsed since most recent repair (i.e. when serviceability is \( S_i \)), \( \tau \) and \( n \) are parameters controlling the deterioration pattern, analogous to \( \rho \) and \( \beta \) in Equation 2.1. Note that \( S = S_f \) is approached only at infinite time. By setting \( S_i = 100\% \) (i.e., pristine) and \( S_f = 0 \) (i.e., worst possible) the resulting serviceability curve can be viewed as a so-called survivor curve (Lytton 1987; Stampley et al. 1995).

Plots of Equation 2.2 over a 25 year period are included in Figure 2.1. Three different \( n \) values (0.5, 1.0, and 2.0) are considered in Figure 2.1(a) for \( \tau = 7 \) years. Three different \( \tau \) values (5, 7 and 9 years) are considered in Figure 2.1(b) for \( n = 1 \). As can be seen, Equation 2.2 is able to describe a pavement that progressively deteriorates - while switching between three different degradation rates. Initially, for a certain time interval, the degradation rate is very small - allowing the pavement to practically remain in pristine conditions. Next, the deterioration rate increases, causing a relatively quick drop in serviceability. Finally, the deterioration rate is arrested, slowing the drop in serviceability. In both charts the solid line indicates an assumed benchmark case, associated with \( n = 1 \) and \( \tau = 7 \) years. This benchmark case depicts a realistic situation for a pavement with an initial serviceability rating of 100\% that deteriorates to 50\% serviceability after 10 years and to a rating of about 25\% after 25 years. Two pavement damage pictures are superposed over the charts, each associated with a different serviceability level. The association is approximate, merely provided to exemplify the physical meaning of the curves. The purpose here is to intuitively
reinforce the link between lower serviceability and infrastructure vulnerability to a hazard event.

Also included in Figure 2.1 are qualitative ratings of infrastructure condition, ranging from “Good” to “Failed”. The descriptive scale is identical to that employed in the Pavement Condition Index (PCI) method (ASTM D6433 or ASTM D5340), a scheme often used by pavement managers (Shahin 2005). For the purpose of the current work a PCI index may be used in place of a serviceability rating, i.e., they are interchangeable.

2.2 Maintenance

The curves in Figure 2.1 essentially represent pavement condition under a no-maintenance situation. When maintenance is applied at some point in time, it changes the shape of the deterioration curve. First, rehabilitation activities appear as a sudden jump in the curve, i.e., an abrupt increase due to improved serviceability. Further, maintenance work alters the subsequent shape of the deterioration curve. Realistically, pavements cannot be preserved at their original as-built serviceability levels throughout the life of the system. Hence, some decline in performance is allowed in the different network components before taking repair actions. Policies for maintaining deteriorating systems have been studied extensively (not necessarily for the pavement discipline), with numerous proposed model types (Wang 2002), e.g., age-based, periodic/sequential, failure/performance/condition-based, cost limited, repair-duration limited, opportunistic, etc.
Figure 2.1. Serviceability curves (Eq. (2)) showing the influence of: (a) $n$ parameter, and (b) $\tau$ parameter. Superposed damage pictures illustrate the physical meaning of condition rating; image source: Federal Highway Administration Pavement Distress Identification Definition Manual (2015)
In practice, pavement repair actions are scheduled according to a condition-based policy (Hajek et al. 2011; Air Force Civil Engineer Center 2014). Typically, a set of intervention rules is pre-stated, triggering a specific maintenance effort on the basis of the component condition level. An intervention rule associated with a high serviceability rating usually requires more frequent repairs but involves only preventive or minor rehabilitation. Triggering intervention at low serviceability levels typically implies that major and costly rehabilitation efforts are necessary. Research on this connection, e.g. Camahan et al. (1987), Madanat and Ben-Akiva (1994), has generally focused on maximizing cost effectiveness by optimizing decisions, such as: (i) how frequently maintenance should be applied; (ii) to what condition a pavement should be allowed to deteriorate before action is taken; and (iii) what best maintenance alternative to take for a given situation. Contributions in this field have also attempted to integrate condition forecasting into the optimization.

Figure 2.2 depicts condition evolution for a pavement under a simplistic threshold-based maintenance policy. The abscissa represents time and the ordinate represents serviceability rating. Starting from an arbitrary “current” rating, the condition is seen to degrade with elapsed time until a predefined threshold level is reached \( S = 60 \% \) in the case shown). This threshold designates a minimal acceptable serviceability rating for the infrastructure being considered. Repair intervention is therefore triggered, raising the rating to \( S = 100 \% \). Then after, the pavement condition continues its decline, triggering a new repair intervention once the threshold is encountered again. This situation is repetitive/cyclic. The depiction in Figure 2.2 is deemed simplistic, because it presumes that the deterioration curve has identical shape
before and after repair, and because the pavement receives treatment at the exact designated timing - assuming all necessary resources are available for the repair. Without loss of generality, these simplifications are adopted for the current work.

Figure 2.2. Illustration of a threshold-based maintenance policy
Chapter 3: Resilience Definition

The literature is replete with qualitative discussions and quantitative methods for measuring system resilience, as well as other related system performance metrics, including: risk, vulnerability, reliability, robustness, flexibility, survivability, etc. See Faturechi and Miller-Hooks (2015) for a synthesis of articles proposing such measures in the context of transportation systems alone. The concept of resilience as adopted and computed herein considers two main features: (i) the system’s innate ability, based on the physical properties and topology/connectivity of its components, to cope with a disruption event that causes physical damage and (ii) the system’s ability to adapt through quick, cost-effective actions that can preserve or restore post-event performance/functionality. Both features are depicted in Figure 3.1, which schematically illustrates system performance vs. time before and after a disruption event; notice the time axis changes scale between pre- and post-event, from months (pre-disruption) to hours (upon disruption). As can be seen, the system’s post-event performance level after a time period with length $T_{\text{max}}$ is composed of two parts: (i) coping capacity - defined as performance level prevailing immediately after disruption; and (ii) adaptive capacity - defined as the improvement in performance level restored during $T_{\text{max}}$ for a given set of repair resources. Ultimately, resilience is defined with respect to a baseline. It is taken as the ratio of post-response system performance level at event time $t$ to pre-event system performance level for link serviceability levels at base time zero.
Figure 3.1(a) illustrates the commonplace assumption of a system that is initially (and at all times) in pristine condition (e.g., Bruneau et al. 2003). On the other hand, Figure 3.1(b) depicts a system with fluctuating performance. This latter case is the non-traditional viewpoint offered herein; it originates from evolving component conditions and varying component age. Consideration and inclusion of component conditions prior to disaster event in the resilience study of a networked pavement is the main contribution of this work. As can be seen, pre-event performance level for the system is imperfect, leading to poorer coping and adaptive capacities than seen in Figure 3.1(a).
Figure 3.1. Approaches to infrastructure resilience: (a) pre-event system performance is timewise constant with all components in pristine condition; and (b) pre-event system performance fluctuates due to non-uniform component conditions

A mathematical modeling approach proposed in Miller-Hooks et al. (2012) is used in this work, wherein resilience is quantified through solution of a nonlinear, two-stage, stochastic program. The stochastic program seeks to maximize the expectation of an indicator representing the resilience of the network (throughput in this case) over
possible disruption scenarios. That is, resilience actions are incorporated in the resilience computation, thus accounting for not only the innate coping capacity of the system, but also post-event adaptability in the disruption event’s immediate aftermath. Optimal mitigation and preparedness actions are determined in the first-stage prior to event realization, and scenario-dependent, optimal, remedial actions are chosen in the second-stage in the form of recourse. Recourse decisions are taken with full knowledge of how the event is realized. Availability, cost and implementation time of recourse options may also depend on the choice of preparedness actions. An integer L-shaped decomposition method is applied to provide exact solution for the problem. This method decouples first- and second-stage decisions, eliminating bilinear terms that are the root of the nonlinearity.

The contribution of this work (i.e. incorporating component conditions in resilience study) starts with failure probabilities with serviceability, the latter being governed by: age, normal deterioration curves, and maintenance policies. Specifically, the probability an adverse event will lead to component failure depends on the component’s serviceability level at the event time, and the ability of the system to provide services depends on its functioning components. Moreover, the cost and time for implementing repair or other restorative options post-event are also functions of pre-event serviceability rating. If a component is deteriorated, the effort required to return it to pristine condition will be greater than if that component were not deteriorated. This is in part because the effectiveness of the restorative options will be diminished once the component has deteriorated to certain levels. This integration of
component condition in resilience computation is described and demonstrated through a case study given next.
Chapter 4: Demonstration on Case Study

4.1 Introduction and Design

A specific case study is employed hereafter to demonstrate and assess the effects and value of incorporating evolving component conditions in resilience quantification. Use is made of a pavement system representing Laguardia Airport’s (LGA’s) taxiway and runway network. This choice builds on previous work (Faturechi et al. 2014), which was motivated by the fact that air transportation is one of fastest growing transportation modes worldwide. It is also driven by the particular sensitivity of airport operations to pavement condition. LGA contains two intersecting runways and supporting taxiways - as depicted in Figure 4.1. These components and their interconnectivity are represented by a 68-node, 104-link network.
Resilience of the LGA pavement network was computed in Faturechi et al. (2014) with an implicit assumption of pristine component condition (pre-event). Figure 4.2 synopsizes the employed modeling approach, and the reader is encouraged to consult Faturechi et al. (2014) for full details. In general terms, the model involves identification of a set of potential directed paths through the airport network for maneuvers between the gates and takeoffs or landings. Despite that each runway can be used in two directions, within a given period of time, runway operations are unidirectional for safety reasons. Thus, the model forces a choice of direction, a so-called runway configuration, within a given time period. If an arc is damaged, its capacity to support the movement of an aircraft is zero; hence, only paths whose constituent arcs are undamaged or repaired can support flow.
<table>
<thead>
<tr>
<th>Objective</th>
<th>$\max E_\xi[Z(\xi)]$, where $Z(\xi) = \max \sum_{w, g, s} \sum_{p \in P_{g,s}} f_p^{g,w,s}(\xi)$</th>
<th>Maximize expected number of takeoffs and landings of small and large aircraft types, i.e. flows, $f$, through the system over all disruption scenarios $\xi$, $g$ runway configurations, $w$-maneuvers, $s$-aircraft types and $P$-active paths (constant denominator in Eq. 3 included for resilience computation)</th>
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<td>Pre-event decision variables:</td>
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<tr>
<td>$\tau_m$</td>
<td>binary variable indicating that $m$ repair crews are employed to support internal repair capabilities ($= 1$ if exactly $m$ are employed and $= 0$ otherwise)</td>
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<tr>
<td>$Y_{e,n}$</td>
<td>binary variable indicating if $n$ units of additional equipment of type $e$ (e.g. rollers, pavers, cutters) are purchased ($= 1$ if provided and $= 0$ otherwise)</td>
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<tr>
<td>Resource limitations</td>
<td>Number of trained repair crews</td>
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<td>Number and type of equipment to keep on site</td>
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<td>Post-event decision variables:</td>
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<tr>
<td>$\pi^\theta(T)$</td>
<td>binary variable indicating whether or not runway configuration $g$ is selected under scenario $\xi$ ($= 1$ if selected, and $= 0$ otherwise)</td>
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<tr>
<td>$\lambda^e_{r,\theta}(\xi), \lambda^i_{a,r}(\xi)$</td>
<td>binary variable indicating whether or not repair action $r$ is taken by external and internal (airport repair team and equipment) resources, respectively, on taxiway $a \in A_1$ under scenario $\xi$ ($= 1$ if taken and $= 0$ otherwise), respectively</td>
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<tr>
<td>$\lambda^e_{a,r}(\xi), \lambda^i_{a,r}(\xi)$</td>
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<td>$f_p^{g,w,s}(\xi)$</td>
<td>post-repair flow rate along path $p$ for runway configuration $g$, maneuver type $w$ and aircraft type $s$ under scenario $\xi$</td>
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<td><strong>Repair period limit</strong></td>
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<td>only takeoffs and landing occurring before $T^{\text{max}}$ counted in resilience</td>
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<td>repair time limitations</td>
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<td><strong>Equipment use restrictions</strong></td>
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<td>use of single equipment piece limited to one location at any point in time</td>
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<td>multiple pieces of equipment can be used at multiple damage sites simultaneously</td>
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<td>outsourcing permitted at a cost</td>
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<td><strong>Post-repair flow restrictions</strong></td>
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<td>arriving and departing flow rates limited to original demand</td>
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<td><strong>Budget limitations</strong></td>
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<td>portion of fixed budget allocated to preparedness (first-stage) decisions</td>
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<td>portion of budget saved for post-disruption event (second-stage) repair actions</td>
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<td>post-event repair actions can be taken internally if resources put in place pre-event</td>
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**Figure 4.2. Overview of stochastic program for airport pavement network resilience computation employed in Faturechi et al. (2014)**
Consequently, for a given budget $B$ and response duration $T^{\text{max}}$, resilience is computed as the ratio $\alpha_{B,T^{\text{max}}}$ of the expected number of landings and takeoffs to a comparable pre-disruption flow rate given by demand $D^{w,s}$ for each maneuver $w$ and aircraft type $s$, over all disaster scenarios $\xi$. As defined in Figure 4.2, $f_{p}^{g,w,s}(\xi)$ is the flow rate of maneuver $w$ for aircraft type $s$ in path $p$ under runway configuration $g$ and scenario $\xi$. 

$$\alpha_{B,T^{\text{max}}} = \frac{E_{\xi}\left[ \sum_{w,s} \sum_{p \in p, s, \xi} f_{p}^{g,w,s}(\xi) \right]}{\sum_{w,s} D^{w,s}}$$  \hspace{1cm} (4.1)$$

The expectation is taken over a set of predicted disaster-meteorological event scenarios that may arise due to any one of a number of hazard event types, whether natural, accidental or malicious, with anticipated occurrence probabilities. First-stage decisions mitigate disaster impact and can support post-event repair opportunities (e.g. availability of materials, repair equipment, trained crews, and contracts with external resources). These decisions are be taken \textit{a priori} with the knowledge that second-stage recourse (repair) decisions will be taken optimally \textit{a posteriori} given the available resources, and knowledge of how the disaster-meteorological event unfolds.

An overview of the computational framework, specified for the case study, is given in Figure 4.3. Similar to Faturechi et al. (2014), the scheme consists of three main modules: (i) scenario generation, (ii) mathematical modeling; and (iii) model solution. As part of the scenario generation, runway and taxiway link failure probabilities were made functions of serviceability as described in Equation 2.2. To capture serviceability levels as a function of component’s age and maintenance plan,
serviceability ratings \( S^a(t) \) were explicitly defined as a function of time \( t \) for each runway or taxiway link \( a \):

\[
S^a(t) = S^a_i - \frac{S^a_f - S^a_i}{\exp\left(\frac{\tau}{t - t^a_m}\right)},
\]

(4.2)

where \( t^a_m \) is the time of last maintenance before time \( t \) which has brought the serviceability of link \( a \) back to \( S^a_i \) at that time (\( t > t^a_m \) at all times). \( S^a_i \) is the initial serviceability condition typically taken as pristine, and \( S^a_f \) is the final (worst possible or ultimate) serviceability rating approached if no repair is applied typically taken as zero.

Each scenario is defined in terms of damage severity and type (climate/geological, operational, natural deterioration, and terrorism), along with current meteorological conditions in terms of temperature, precipitation and visibility conditions. Meteorological conditions are described in terms of temperature, visibility, wind velocity and precipitation, which might affect potential damage causes and types. The causes also affect damage location and distribution of damage in multiple locations over the pavement network. The likelihood of an event falling within any of these causal categories depends on the geographical characteristics of the airport. A host of damage-weather scenarios are possible. To capture correlations between damage characteristics and meteorological conditions, conditional probabilities are employed in generating scenarios. The probability of each scenario is assumed to be known \textit{a priori}. Specifically, let \( p_a(\xi_0) \), \( p(\xi_0 \mid d) \), \( p(d \mid m) \) and \( p(m) \), be the probability of
scenario $\xi_0$, probability of scenario given disruption type $d$, probability of disaster type given meteorological condition $m$, and probability of meteorological condition $m$ for the given geographical location, respectively. Then,

$$p_a(\xi_0) = p(s \mid d) \cdot p(d \mid m) \cdot p(m),$$  \hspace{1cm} (4.3)

The failure probability $p_a(\xi_i)$ of link $a$, given disruption-meteorological event $\xi_i$ arising at time $t$, is related to $S^a(t)$ as follows:

$$p_a(\xi_i) = (1 + c(1 - S^a(t)))p_a(\xi_0),$$  \hspace{1cm} (4.4)

where $p_a(\xi_0)$ is the failure probability of link $a$ at 100% serviceability (i.e. under pristine conditions) for given event type. As can be seen, the sought failure probability is governed by a positive proportionality constant $c$. This is a newly introduced parameter that links serviceability ratings to the formulation. Higher values of $c$ infer greater influence of component condition on failure probabilities. Note that if $c$ is set large enough, it is possible that a probability greater than one would be generated; a ceiling of probability-one is therefore assumed. If $S^a(t) = 100\%$ at all times, then the influence of $c$ is annulled, yielding the familiar assumption in the resilience literature: $p_a(\xi_i) = p_a(\xi_0)$. Similarly, the damage severity of link $a$ is captured through repair action implementation cost and time, which are also formulated as a function of the link’s serviceability level:

$$b_a(\xi_i) = (1 + c(1 - S^a(t)))b_a(\xi_0),$$  \hspace{1cm} (4.5a)

$$q_a(\xi_i) = (1 + c(1 - S^a(t)))q_a(\xi_0),$$  \hspace{1cm} (4.5b)
in which $b_a(\xi_0)$ and $q_a(\xi_0)$ are implementation cost and time of repair actions in link $a$ with a serviceability rating of 100%. Their values depend on the event type. While the $c$ parameter was taken as identical across Equations 4.4 and 4.5, in a more general formulation this presumption may be relaxed.

Given possible weather conditions and probability of their occurrences specific to LGA, disruption-meteorological events, resulting damage types (e.g. cracking, disintegration, distortion, loss of skid resistance), potential damage extent in terms of maximum number of affected segments, and repair actions required in each case were generated. Each disruption meteorological event gives a set of link failure probabilities which are used to randomly generate operational (one) or failed (zero) link states to create each disruption-meteorological scenario. An overview of the scenario generation process is given in Figure 4.3. Conditional probabilities capture correlations between damage characteristics and meteorological conditions. Thus, the result of scenario generation is the set of disruption-meteorological events with one/zero values for link functionality and characteristics associated to that disruption event such as the required repairs, available repairs, etc. Ultimately, resilience was assessed at 6-month intervals over a 15-year time horizon during which network component conditions continually evolved.
Figure 4.3. Diagram of case study resilience quantification
4.2 Case Study Specifics

Presented in what follows are modeling details involved in resilience quantification of the LGA case study. First, a budget $B$ for emergency preparedness and response of $\$25,000$ was assumed. Also, $T^{\text{max}}$ was set to 8 hours, and $c$ in Equations 4.4 and 4.5 was taken to equal 1.5 (in lieu of relevant information from other sources this choice was based on preliminary run results). Resilience is measure of a system’s innate coping capacity and ability to adapt when confronted with a challenge. Thus, resilience is conceptualized here to include adaptive actions that can be taken quickly and relatively cheaply. Higher monetary and time budgets can be used; however, a system that would require significant resources for continued operations might not be considered resilient. Benchmark deterioration curve parameter set was assumed to hold for both taxiways and runways; with reference to Equation 4.2 these are $n=1$ and $\tau = 7$ years. Two separate threshold-based maintenance plans (MPs) were considered. In MP1 rehabilitation actions are taken whenever runway serviceability reaches 80% and taxiway serviceability reaches 60%. This is consistent with a repair interval of about 4.0 and 7.5 years, respectively. In MP2 the rehabilitation thresholds were 60% for runways and 40% for taxiways. Respectively, these imply repair intervals of about 7.5 and 13.5 years.

With both MPs, runways are maintained at higher average levels than are taxiways. MP1 imposes more stringent rehabilitation demands as compared to MP2, and represents an airport pavement network that is, on average, in better condition. Moreover, the age of each runway at the beginning of the resilience analysis period was randomly set given $\sim\text{U}[0,4.0]$ and $\sim\text{U}[0,7.5]$ years for MP1 and MP2,
respectively. Similarly, the starting age of the taxiways was randomly set given $\sim U[0,7.5]$ and $\sim U[0,13.5]$ years for MP1 and MP2, respectively. This procedure generated a realistic situation where the serviceability across the network is non-uniform.

MP1 and MP2 parameters are summarized in Table 4.1 which lists the initial ages of the different network components, as well as their associated serviceability rating and maintenance threshold. As may be seen, taxiways were grouped based on their orientation relative to the runways: parallel and perpendicular. Such distinction has some operational implication that is captured (internally) by the model. Condition evolution of taxiways and runways according to MP1 is plotted in Figure 5.1(a). Similar information for MP2 is included in Figure 5.1(c). Each chart includes four lines, representing changes in infrastructure serviceability over a 15 year period. Starting levels are dissimilar per Table 4.1 values. As can be seen, full rehabilitation to pristine conditions is presumed after a threshold is encountered, generating a repetitive pattern. Because starting serviceability levels are different, and because the rehabilitation threshold for taxiways and runways are different, the condition of the system at any point in time is spatially nonuniform.
<table>
<thead>
<tr>
<th>Infrastructure Component</th>
<th>Maintenance Plan 1 (MP1)</th>
<th>Maintenance Plan 2 (MP2)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Starting age (years)</td>
<td>Starting Serviceability rating $S_a(0)$</td>
</tr>
<tr>
<td>Runway 1</td>
<td>3.1</td>
<td>90%</td>
</tr>
<tr>
<td>Runway 2</td>
<td>1.7</td>
<td>98%</td>
</tr>
<tr>
<td>Taxiway-perpendicular</td>
<td>4.5</td>
<td>79%</td>
</tr>
<tr>
<td>Taxiway-parallel</td>
<td>6.2</td>
<td>68%</td>
</tr>
</tbody>
</table>
Chapter 5: Results and Analysis

The resilience indicators for the case study, calculated through Equation 4.1, are presented in Figure 5.1. Charts 5.1(b) and 5.1(d) display resilience calculation outcomes associated with MP1 (Figure 5.1(a)) and MP2 (Figure 5.1(c)), respectively. Each chart contains 31 values covering an analysis period of 15 years at 6-month intervals. The resilience values fluctuate due to differences in component conditions between the different evaluation times, and also because of the statistical nature of generating scenarios. Specifically, each point in the figure is computed from an average performance value over 360 randomly generated disruption-meteorological scenarios. Model runs might be repeated over additional sets of randomly generated scenarios to produce a range of resilience estimates or a single expectation over a larger set of possibilities.
Figure 5.1. Case study results: (a) evolution of serviceability according to MP1, (b) consequent system resilience under MP1, (c) evolution of serviceability according to MP2, and (d) consequent system resilience under MP2

Two horizontal lines are superposed on each resilience chart, forming bands that encapsulate all run results. These lines represent a single upper bound (UB) evaluation and a single lower bound (LB) evaluation of the system resilience plus (or minus) two standard deviations that were calculated based on the spread in each case. The UB case denotes system resilience level with all components in pristine condition (pre-event). It is therefore unaffected by MP specifics. The LB case denotes a system resilience level with all components at their worst allowable condition simultaneously - according to the governing MP threshold. This LB value will differ between MPs and in the case shown is slightly higher for the more stringent MP1. Note that while pristine conditions are presumed in the computation of the resilience upper bound, and worst acceptable serviceability for the lower bound, the resilience bound values are
computed over 360 randomly generated disruption-meteorological scenarios. Thus, they may vary as a function of the scenario generation output. The difference between UB and LB is about 17% for MP1 and about 20% for MP2. This difference directly depends on the value chosen for $c$ in Equations 4.4 and 4.5 and the set of generated scenarios.

Overall, Figure 5.1 reveals that the network resilience changes over time between the upper and lower bounds with values that depend, among other factors, on link conditions, link natural deterioration pattern, and prevailing MPs.
Chapter 6: Conclusions and Future Work

This work is concerned with quantifying the resilience of an airport pavement network while allowing for evolving component conditions. Application to a case study demonstrated that resilience is impacted by the initial condition of the infrastructure links, by their natural deterioration trends, and by prevailing maintenance policies and actions. The impact found was significant, indicating the need and value for such an approach. The method employed is flexible and can be further refined or compounded by, for example: (i) assigning different maintenance thresholds to different components or incorporating other repair policies; (ii) optimizing maintenance actions rather than assuming a given schedule or protocol; or (iii) using any one of a number of serviceability models, including stochastic methods for predicting future condition.

Note that for other pavement networks, such as a roadway network, the adopted resilience metric would be modified. In the case of the roadway network, a measure based on vehicular throughput or travel time/delay could be employed. In the latter case, a bi-level programming formulation might be adopted where the lower level would provide link travel time estimates given post-event roadway conditions and chosen resilience actions. Refer to Faturechi and Miller-Hooks (2015) for roadway resilience estimation in which pristine conditions are implicitly assumed; such estimates account for user response to system changes.

Even though a specific case and type of application were considered, the findings here are of general nature; they imply that earlier resilience works report UB values (refer to Figure 5.1). In other words, best-case resilience estimates are typically provided.
For the current formulation this is equivalent to annulling $c$ in Equations 4.4 and 4.5. Moreover, in light of evolving component conditions, the definition of resilience may also require reexamination. Resilience is typically quantified relative to a pre-event baseline signifying pristine system performance. Because component conditions are allowed to evolve, pristine performance is not realistically achievable, while at the same time pre-event performance fluctuates (see Figure 3.1).

Commonly, optimization of MPs is based on life cycle cost analyses. A continuation of this work may include MPs that are associated with resilience quantification, i.e., investigating MPs in terms of effects on resilience. One option in this connection is making the MP a decision variable, with its own budget, and integrating in the decision process for preparedness (current model did not include maintenance cost and resources). Timing and location of repair decisions was not considered in the employed MP, but the approach here allows testing such strategies (e.g., Medury and Madanat 2013). So doing can lead to new implications for maintenance budget allocation/prioritization. Also of interest is performing an in-depth parametric/sensitivity analysis of each resilience calculation. This means investigating the solution details for resilience by event categories, differences in division of budget between preparedness and response, or any other changes in decision variables. These aspects will serve as topics for future work.
Appendix I: Notation and Formulation

The notation and formulation used in this paper are included here. They are extracted from the work of Faturechi et. al (2014). For description of constraints and equations refer to Faturechi et. al (2014).

Notation:
- **A**: set of links \((A = A_1 \cup A_2 \cup A_3)\), where \(A_1\) is the set of taxiways, \(A_2\) is the set of runways, and \(A_3\) is the set of added dummy links
- **G**: set of runway configurations \(g\)
- **\(A^c_{1,g}\)**: subset of taxiways connected to a runway \(\hat{a} \in A_2\) (entrance/exit taxiways)
- **\(A_2^b\)**: subset of runways that are active under configuration \(g\)
- **\(l_{\hat{a}}\)**: set of segments of runway \(\hat{a} \in A_2\)
- **\(I_{\hat{a}}^a \subset I_{\hat{a}}\)**: subset of segments of runway \(\hat{a} \in A_2\) following (leading to) entrance (exit) taxiway \(a \in A^c_{1,\hat{a}}\)
- **\(O, D\)**: super source and sink nodes
- **\(W\)**: set of maneuver types \(w \in W = \{arr, dep\}\) for arrival and departure maneuvers between nodes \(O\) and \(D\), respectively
- **\(R\)**: set of repair actions \(r\)
- **\(E\)**: set of equipment types \(e\)
- **\(N_{ae}\)**: maximum number of equipment type \(e\) that could possibly be provided
- **\(M\)**: maximum number of teams that might be deployed
- **\(S\)**: set of aircraft classes (sizes) \(s\)
- **\(Y_{e,n}\)**: required storage space for \(n\) pieces of equipment type \(e\)
- **\(Y\)**: total available storage space
- **\(p_{g,w,s}\)**: set of active paths \(p\) for runway configuration \(g\), maneuver type \(w\) and aircraft class \(s\)
- **\(D_{w,s}\)**: original demand for maneuver type \(w\) and aircraft class \(s\) (arrival and departure demands)
- **\(F_{\upsilon,xc}\)**: capacity envelop for taxiway \(a \in A_1\) representing directional flow tradeoff
- **\(c_{\upsilon,a}(\xi)\)**: capacity of taxiway \(a \in A_1\) for both directions \(L\) and \(R\) under meteorological conditions of scenario \(\xi\)
- **\(F_{\upsilon,rc}\)**: overall capacity envelop for runway configuration \(g\) representing total arrival and departure flow tradeoff
- **\(F_{\upsilon,a}\)**: capacity envelop of runway \(\hat{a} \in A_2\) representing arrival and departure flow tradeoff of that individual runway
- **\(C\)**: large scalar
- **\(\delta_{ap}^{k,g,w,s}\)**: taxiway path-link incidence (=1 if path \(p\) for runway configuration \(g\) with maneuver type \(w\) and aircraft class \(s\) uses direction \(k\) of taxiway \(a \in A_1\), and =0 otherwise)
- **\(\delta_{ap}^{g,w,s}\)**: runway path-link incidence (=1 if path \(p\) for runway configuration \(g\) with maneuver type \(w\) for aircraft class \(s\) uses runway \(\hat{a} \in A_2\), and =0 otherwise)
- **\(\rho_{\xi,r}\)**: scenario-repair relationship parameter, which is set to 1 if repair action \(r\) can be taken under the meteorological conditions of scenario \(\xi\), and 0 otherwise.
- **\(\bar{\rho}_{e,r}\)**: equipment-repair relationship parameter, which is set to 1 if equipment \(e\) is needed for a team to take repair action \(r\), and 0 otherwise.
- **\(b_{tm}\)**: cost of employing \(m\) teams \((m = 0, 1, ... M)\)
- **\(b_{e,n}\)**: cost of providing \(n\) pieces of equipment type \(e\)
- **\(b_{a,\upsilon}(\xi), q_{a,\upsilon}(\xi)\)**: implementation cost and time of repair action \(\upsilon\) by external resources in taxiway \(a \in A_1\) under the meteorological conditions of scenario \(\xi\), respectively
- **\(b_{a,\upsilon}(\xi)\)**: implementation cost and time of repair action \(\upsilon\) by internal resources (employed teams and equipment) in taxiway \(a \in A_1\) under the meteorological conditions of...
scenario $\xi$, respectively

$\ell_{a_{ir}}^\text{ex} (\xi), q_{a_{ir}}^\text{ex} (\xi) = \text{implementation cost and time of repair action } r \text{ by external resources in segment } i \text{ of runway } a \in A_2 \text{ under the meteorological conditions of scenario } \xi$, respectively

$\ell_{a_{ir}}^\text{in}, q_{a_{ir}}^\text{in} (\xi) = \text{implementation cost and time of repair action } r \text{ by internal resources (employed teams and equipment) in segment } i \text{ of runway } a \in A_2 \text{ under the meteorological condition of scenario } \xi$, respectively

$b_{a_{ir}}^\text{m}, b_{a_{ir}}^\text{m} (\xi) = \text{maintenance cost of taxiway } a \in A_1 \text{ and segment } i \text{ of runway } a \in A_2 \text{ if repair action } r \text{ is taken, respectively}$

$\tau_{\max} (\xi) = \text{maximum allowed repair time under scenario } \xi$

$B = \text{total budget}$

$\varphi_a (\xi), \Phi_a (\xi) = \text{pre- and post-repair damage state of taxiway } a \in A_1 \text{ under scenario } \xi (=1 \text{ if functional, and } =0 \text{ otherwise), respectively}$

$\varphi_{ai} (\xi), \Phi_{ai} (\xi) = \text{pre- and post-repair damage state of segment } i \text{ of runway } a \in A_2 \text{ under scenario } \xi (=1 \text{ if functional, and } =0 \text{ otherwise), respectively}$

$l_{ai}^w = \text{length of runway segments } i \text{ of runway } a \in A_2$

$l_{a_{ir}}^w = \text{MOS requirements (minimum required length of runways for maneuver type } w \text{ and aircraft class } s \text{ to use that runway)}$

$l_{a, w, s}^w = \text{length of consecutive of post-repair active segments of runway } a \in A_2 \text{ following (leading to) entrance (exit) taxiway } a \in A_2 \text{ under scenario } \xi$

$s_{a, w, s} (\xi) = \text{binary variable indicating whether or not } l_{a, w, s}^w (\xi) \text{ is longer than } l_{a, w, s}^{\min}$\text{ of maneuver type } w \text{ and aircraft type } s \text{ under scenario } \xi (=1 \text{ if longer, and } =0 \text{ otherwise)}$

Pre-event decision variables:

$\tau_m = \text{binary variable indicating that } m \text{ teams are employed } (=1 \text{ if exactly } m \text{ teams are employed and } =0 \text{ otherwise)}$

$\gamma_{e, n} = \text{binary variable indicating if } n \text{ units of equipment type } e \text{ are purchased } (=1 \text{ if provided and } =0 \text{ otherwise)}$

Post-event decision variables:

$\pi_g (\xi) = \text{binary variable indicating whether or not runway configuration } g \text{ is selected under scenario } \xi (=1 \text{ if selected, and } =0 \text{ otherwise)}$

$\lambda_{a_{ir}}^\text{ex} (\xi), \lambda_{a_{ir}}^\text{in} (\xi) = \text{binary variable indicating whether or not repair action } r \text{ is taken by external and internal (airport repair team and equipment) resources, respectively, on taxiway } a \in A_1 \text{ under scenario } \xi (=1 \text{ if taken and } =0 \text{ otherwise), respectively}$

$\lambda_{a_{ir}}^\text{ex} (\xi), \lambda_{a_{ir}}^\text{in} (\xi) = \text{binary variable indicating whether or not repair action } r \text{ is taken by external and internal resources, respectively, on segment } i \text{ of runway } a \in A_2 \text{ under scenario } \xi (=1 \text{ if taken and } =0 \text{ otherwise), respectively}$

$f_p^{g, w, s} (\xi) = \text{post-repair flow rate along path } p \text{ for runway configuration } g, \text{ maneuver type } w \text{ and aircraft type } s \text{ under scenario } \xi$

Formulation overview and details:

$$\max E_{\xi} [Z(\xi)] \text{ s.t. \{resource limitations: (4)-(8)}, \quad (1)$$

where

$$Z(\xi) = \max \sum_{w, g, s} \sum_{p \in P} f_p^{g, w, s} (\xi) \quad (2)$$

(Taxiway capacity estimation: (9)-(16)
Runway capacity estimation: (17)-(20)
Operational constraints: (21)-(24,1,2)
Runway configuration selection: (25)-(27)
Taxiway/runway segment post-repair damage states: (28)-(32)
Repair period limit: (33)-(36)
Budget and post-repair flow restrictions: (37)-(39)

\[ \alpha_{B,T_{\text{max}}} = \frac{E_{t} \sum_{wg} \sum_{wpgw} f_{p}^{g_{w},s} \phi_{w}^{g_{w},s}(\xi)}{\sum_{w} D_{w,s}}. \]  
\[ \sum_{m} \tau_{m} \leq 1 \]  
\[ \sum_{n} Y_{e,n} \leq 1, \quad \forall e \in E \]  
\[ \sum_{e,n} Y_{e,n} \leq Y \]  
\[ \tau_{m} \in \{0,1\}, \quad m = 1, \ldots, M \]  
\[ Y_{e,n} \in \{0,1\}, \quad \forall e \in E, n = 1, \ldots, N_{e} \]  
\[ c_{a}(\xi) = \frac{v_{a}(\xi)}{a_{\text{max}}(\xi)}, \quad \forall a \in A_{1} \]  
\[ x_{a}^{k,g} = \sum_{w} \sum_{p \in pg_{w,s}} d_{a,p}^{k,g_{w},s} f_{p}^{g_{w},s}(\xi), \quad \forall g \in G, a \in A_{1}, k \in \{k_{+}, k_{-}\} \]  
\[ x_{a}^{k+g}(\xi) = \beta_{a,1}^{2} + \beta_{a,2}^{1} + [c_{a}(\xi) - \frac{2a_{1}}{a_{\text{max}}(\xi)}](\beta_{a,2}^{2} + \beta_{a,3}^{1}) + \beta_{a,3}^{2}, \quad \forall g \in G, a \in A_{1} \]  
\[ c_{a}(\xi) \beta_{a,3}^{2}, \]  
\[ x_{a}^{k-g}(\xi) \leq c_{a}(\xi) \beta_{a,1}^{2} + [c_{a}(\xi) - \frac{2a_{1}}{a_{\text{max}}(\xi)}](\beta_{a,2}^{2} + \beta_{a,3}^{1}) + \beta_{a,2}^{2} + \beta_{a,3}^{2}, \quad \forall g \in G, a \in A_{1} \]  
\[ \beta_{a,v}^{1} + \beta_{a,v}^{2} = \psi_{a,v}, \quad \forall a \in A_{1}, \quad v \in \{1,2,3\} \]  
\[ \sum_{v=1}^{3} \psi_{a,v} = 1, \quad \forall a \in A_{1} \]  
\[ \psi_{a,v} \in \{0,1\}, \quad \forall a \in A_{1}, \quad v \in \{1,2,3\} \]  
\[ x_{a}^{k,g} \leq c_{a}(\xi) \Phi_{a}(\xi), \quad \forall g \in G, a \in A_{1}, k \in \{k_{+}, k_{-}\} \]  
\[ x_{a}^{g_{w}}(\xi) = \sum_{a} \sum_{p \in pg_{w,s}} \sum_{a \in A_{2}} d_{a,p}^{g_{w},s} f_{p}^{g_{w},s}(\xi), \quad \forall g \in G, w \in \{\text{arr}, \text{dep}\} \]  
\[ x_{a}^{g_{w},s}(\xi) = F_{a}^{oc}[x_{a}^{g_{w},s}(\xi)], \quad \forall g \in G \]  
\[ x_{a}^{g_{w},s}(\xi) = F_{a}^{rc}[x_{a}^{g_{w},s}(\xi)], \quad \forall g \in G, \hat{a} \in A_{2}, w \in \{\text{arr}, \text{dep}\} \]  
\[ x_{a}^{g_{w},s}(\xi) \leq C_{a}^{w,s}(\xi), \quad \forall a \in A_{1}, \hat{a} \in A_{2}, k \in \{k_{+}, k_{-}\}, g \in G, w \in W, s \in S \]
\[ l_{w,s}^{\min, w,s}(\xi) \leq l_{a,\hat{a}}(\xi) \quad \forall w \in W, s \in S, a \in A_{1,\hat{a}}, \hat{a} \in A_2 \quad (22) \]

\[ o_{w,a}(\xi) \in \{0,1\} \quad \forall w \in W, s \in S, a \in A_1 \quad (23) \]

\[ l_{a,\hat{a}}(\xi) = \sum_{o \in l}_{a}^{\hat{a}}[\Pi_{j=1}^{0} \Phi_{a_j}(\xi)]l_{a_0}^{u} \quad \forall o \in l_{a}^{\hat{a}}, a \in A_{1,\hat{a}}, \hat{a} \in A_2 \quad (24) \]

\[ \Phi_{a_{i',t'+1,...,o}}(\xi) = \Pi_{j=1}^{0} \Phi_{a_j}(\xi), \quad \forall o \in l_{a}^{\hat{a}}, a \in A_{1,\hat{a}}, \hat{a} \in A_2 \]

\[ l_{a,\hat{a}}(\xi) = \sum_{o \in l}_{a}^{\hat{a}}l_{a_0}^{u} \Phi_{a_{i',t'+1,...,o}}(\xi), \quad \forall o \in l_{a}^{\hat{a}}, a \in A_{1,\hat{a}}, \hat{a} \in A_2 \quad (24-1) \]

\[ \Phi_{a_{i',t'+1,...,o}} \leq \Phi_{a_j}(\xi), \quad \forall j \in \{i', i^{*} + 1,..., o\}, o \in l_{a}^{\hat{a}}, a \in A_{1,\hat{a}}, \hat{a} \in A_2 \quad (24-2) \]

\[ \Sigma_{g,S} \sum_{p \in P_{g, w,s}} f_{p}^{g, w,s}(\xi) \leq C \pi^{g}(\xi), \quad \forall g \in G \quad (25) \]

\[ \Sigma_{g} \pi^{g}(\xi) = 1 \quad (26) \]

\[ \pi^{g}(\xi) \in \{0,1\}, \quad \forall g \in G \quad (27) \]

\[ \Phi_{a}(\xi) = [1 - \varphi_{a}(\xi)]\Sigma_{r} \rho_{x,r} \cdot [\lambda_{a,r}^{in}(\xi) + \lambda_{a,r}^{ex}(\xi)] + \varphi_{a}(\xi), \quad \forall a \in A_{1} \quad (28) \]

\[ \Phi_{a_{i}}(\xi) = [1 - \varphi_{a_{i}}(\xi)]\Sigma_{r} \rho_{x,r} \cdot [\lambda_{a_{i},r}^{in}(\xi) + \lambda_{a_{i},r}^{ex}(\xi)] + \varphi_{a_{i}}(\xi) \quad \forall a_{i} \in A_{2}, i \in I_{a} \quad (29) \]

\[ \lambda_{a,r}^{in}(\xi), \lambda_{a,r}^{ex}(\xi), \lambda_{a_{i},r}^{ex}(\xi), \lambda_{a_{i},r}^{in}(\xi) \in \{0,1\}, \quad \forall a \in A_{1}, \hat{a} \in A_{2}, i \in I_{a}, r \in R \]

\[ \Sigma_{r} \rho_{x,r} \cdot [\lambda_{a,r}^{ex}(\xi) + \lambda_{a_{i},r}^{in}(\xi)] \leq 1, \quad \forall a \in A_{1} \quad (31) \]

\[ \Sigma_{r} \rho_{x,r} \cdot [\lambda_{a_{i},r}^{ex}(\xi) + \lambda_{a_{i},r}^{in}(\xi)] \leq 1, \quad \forall a_{i} \in A_{2}, i \in I_{a} \quad (32) \]

\[ \sum_{a \in A_{1}, r} \rho_{x,r} \rho_{x,r} q_{a_{i},r}^{in}(\xi) \lambda_{a_{i},r}^{in}(\xi) + \sum_{a \in A_{2}, i, r} \rho_{x,r} \rho_{x,r} q_{a_{i},r}^{in}(\xi) \lambda_{a_{i},r}^{in}(\xi) \leq \tau_{max}(\xi) \cdot \sum_{n \in N_{e}} n_{y_{e,n}}, \quad \forall e \in E \quad (33) \]

\[ \sum_{a \in A_{1}, r} \rho_{x,r} q_{a_{i},r}^{ex}(\xi) \lambda_{a_{i},r}^{ex}(\xi) + \sum_{a \in A_{2}, i, r} \rho_{x,r} q_{a_{i},r}^{ex}(\xi) \lambda_{a_{i},r}^{ex}(\xi) \leq \tau_{max}(\xi) \cdot \sum_{m \in m_{t_{m}}} \quad (34) \]

\[ \Sigma_{r} \rho_{x,r} q_{a_{i},r}^{ex}(\xi) \lambda_{a_{i},r}^{ex}(\xi) \leq \tau_{max}(\xi), \quad \forall a \in A_{1} \quad (35) \]

\[ \Sigma_{r} \rho_{x,r} q_{a_{i},r}^{ex}(\xi) \lambda_{a_{i},r}^{ex}(\xi) \leq \tau_{max}(\xi), \quad \forall a_{i} \in A_{2}, i \in I_{a} \quad (36) \]

\[ \Sigma_{h} \rho_{x,r} \rho_{x,r} q_{a_{i},r}^{ex}(\xi) \lambda_{a_{i},r}^{ex}(\xi) \leq B \quad (37) \]

\[ \Sigma_{p \in P_{g, w,s}} f_{p}^{g, w,s}(\xi) \leq D_{w,s}, \quad \forall g \in G, w \in W, s \in S \quad (38) \]

\[ f_{p}^{g, w,s}(\xi) \geq 0, \quad \forall g \in G, w \in W, s \in S, p \in P_{g, w,s} \quad (39) \]
Appendix II: Model Inputs and Assumptions

Table A.II. 1. Capacity envelopes for different runway configurations and visibility conditions (Faturechi et. al, 2014)

<table>
<thead>
<tr>
<th>Runway configuration</th>
<th>Capacity envelopes (aircraft per hour)</th>
<th>VFR</th>
<th>IFR</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Arrival</td>
<td>35</td>
<td>32</td>
</tr>
<tr>
<td></td>
<td>Departure</td>
<td>45</td>
<td>42</td>
</tr>
<tr>
<td>4</td>
<td>4</td>
<td>(40, 35)</td>
<td></td>
</tr>
<tr>
<td>13</td>
<td>13</td>
<td>(38, 32)</td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>13</td>
<td>(48, 35)</td>
<td></td>
</tr>
<tr>
<td>22</td>
<td>13</td>
<td>(45, 35)</td>
<td></td>
</tr>
</tbody>
</table>

Table A.II. 2. Disruption events, probabilities and resulting damage (Faturechi et. al, 2014)

<table>
<thead>
<tr>
<th>Disruption event</th>
<th>Probability</th>
<th>Alligator cracking</th>
<th>Block cracking</th>
<th>Transverse cracking</th>
<th>Jet Blast</th>
<th>Raveling</th>
<th>Rutting</th>
<th>Potholes</th>
<th>Single crater</th>
<th>Slippery surface</th>
<th>Bleeding</th>
</tr>
</thead>
<tbody>
<tr>
<td>Extreme climatic or geologic event</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Flood</td>
<td>0.095</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-(20)</td>
<td>-</td>
</tr>
<tr>
<td>Snow/ice</td>
<td>0.050</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-(5)</td>
<td></td>
</tr>
<tr>
<td>Very hot</td>
<td>0.045</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>(2)</td>
<td>-</td>
<td>-</td>
<td>(4)</td>
<td></td>
</tr>
<tr>
<td>Operational events</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Oil spill</td>
<td>0.280</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td></td>
</tr>
<tr>
<td>Overloading</td>
<td>0.220</td>
<td>(10)</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td></td>
</tr>
<tr>
<td>Jet Blast</td>
<td>0.190</td>
<td>-</td>
<td>-</td>
<td>(3)</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td></td>
</tr>
<tr>
<td>Intentional malicious acts</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Guided attack</td>
<td>0.060</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>- (2*)</td>
<td>-</td>
<td>-</td>
<td>(3)</td>
<td>-</td>
</tr>
<tr>
<td>Unguided attack</td>
<td>0.060</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>- (10)</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td></td>
</tr>
</tbody>
</table>

*Indicates that consecutive segments affected; otherwise, damage need not be adjoining.
### Table A.II. 3. Repair equipment (Faturechi et. al, 2014)

<table>
<thead>
<tr>
<th>Identification #</th>
<th>Equipment</th>
<th>Cost ($/year)</th>
<th>Identification #</th>
<th>Equipment</th>
<th>Cost ($/year)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Small asphalt paver</td>
<td>8100</td>
<td>11</td>
<td>Tack coat sprayer</td>
<td>1800</td>
</tr>
<tr>
<td>2</td>
<td>Mechanical sweeper</td>
<td>8500</td>
<td>12</td>
<td>Seal injector/melter</td>
<td>1500</td>
</tr>
<tr>
<td>3</td>
<td>Small milling machine</td>
<td>6500</td>
<td>13</td>
<td>Crack chasing saw</td>
<td>2700</td>
</tr>
<tr>
<td>4</td>
<td>Small asphalt roller</td>
<td>1400</td>
<td>14</td>
<td>Small mixer</td>
<td>1350</td>
</tr>
<tr>
<td>5</td>
<td>Asphalt cutter</td>
<td>1700</td>
<td>15</td>
<td>Water pump</td>
<td>1350</td>
</tr>
<tr>
<td>6</td>
<td>Salt Sprinkler</td>
<td>2550</td>
<td>16</td>
<td>Large milling machine</td>
<td>9500</td>
</tr>
<tr>
<td>7</td>
<td>Snow shovel</td>
<td>4800</td>
<td>17</td>
<td>Vibratory roller</td>
<td>2210</td>
</tr>
<tr>
<td>8</td>
<td>Front loader</td>
<td>8160</td>
<td>18</td>
<td>Motor grader</td>
<td>25000</td>
</tr>
<tr>
<td>9</td>
<td>Backhoe</td>
<td>13600</td>
<td>19</td>
<td>Large asphalt paver</td>
<td>32000</td>
</tr>
<tr>
<td>10</td>
<td>Dump truck</td>
<td>11650</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

### Table A.II. 4. Repair actions, implementation costs and execution times (Faturechi et. al, 2014)

<table>
<thead>
<tr>
<th>Damage types to be repaired</th>
<th>Repaired Internally</th>
<th>Repaired externally</th>
<th>Weather-dependent multiplier for repair duration and costs</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Equipment set</td>
<td>Duration (hr)</td>
<td>Cost ($)</td>
</tr>
<tr>
<td>Alligator cracking</td>
<td>1,2,4,8,10,15,16</td>
<td>5</td>
<td>2510</td>
</tr>
<tr>
<td>Block cracking</td>
<td>2,11,12</td>
<td>2</td>
<td>736</td>
</tr>
<tr>
<td>Transverse cracking</td>
<td>2,11,12</td>
<td>2</td>
<td>736</td>
</tr>
<tr>
<td>Jet Blast</td>
<td>2,4,5,8,9,10,15</td>
<td>4</td>
<td>1912</td>
</tr>
<tr>
<td>Raveling</td>
<td>2,4,5,8,9,10,15</td>
<td>4</td>
<td>1912</td>
</tr>
<tr>
<td>Rutting</td>
<td>2,4,5,8,9,10,15</td>
<td>4</td>
<td>1912</td>
</tr>
<tr>
<td>Array of small potholes</td>
<td>1,2,4,5,6,16</td>
<td>3</td>
<td>1407</td>
</tr>
<tr>
<td>A single crater</td>
<td>1,2,3,4,5,6,7,15,16,17,19</td>
<td>6</td>
<td>4374</td>
</tr>
<tr>
<td>Slippery surface</td>
<td>2,4,14,15,18</td>
<td>1</td>
<td>461</td>
</tr>
<tr>
<td>Bleeding</td>
<td>2,4,5,6,13,17</td>
<td>3</td>
<td>1665</td>
</tr>
</tbody>
</table>
References


