Measurement of Tensor Polarization in Elastic Electron-Deuteron Scattering in the Momentum-Transfer Range $3.8 \leq q \leq 4.6$ fm$^{-1}$


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The tensor polarization $t_{20}$ of the recoil deuteron in elastic $e$-$d$ scattering has been measured for three values of four-momentum transfer, $q = 3.78$, 4.22, and 4.62 fm$^{-1}$. The data have been used to locate the first node in the charge monopole form factor of the deuteron at $q = 4.39 \pm 0.16$ fm$^{-1}$. The results for $t_{20}$ are in reasonable agreement with expectations based on the nucleon-meson description of nuclear dynamics.

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The electromagnetic structure of the spin-1 deuteron is described by three form factors: charge monopole $F_C$, charge quadrupole $F_Q$, and magnetic dipole $F_M$. Cross-section measurements in elastic $e$-$d$ scattering yield the structure functions $A(F_C,F_Q,F_M^2)$ and $B(F_M)$ [1] but do not allow the separation of $F_C$ and $F_Q$. Therefore, the measurement of another observable is necessary. We have measured the tensor polarization of the recoil deuteron [2]:

$$ t_{20} = -\sqrt{2} \left[ x(x+2) + y/2 \right] / \left[ 1 + 2(x^2 + y) \right], $$

where $x = \frac{3}{2} \eta F_Q/F_C$, $y = \frac{3}{2} \eta f(\theta_e) F_Q/F_C$, $f(\theta_e) = \frac{1}{2} + (1 + \eta) \tan^2(\theta_e/2)$, and $\eta = q^2/4M_d^2$; $q$ is the four-momentum transfer, $M_d$ is the deuteron mass, and $\theta_e$ is the electron-scattering angle in the laboratory frame. The quantity $t_{20}(y = 0)$, derived from Eq. (1) by neglecting the magnetic contribution, is often used in the literature. The measurements reported here cover a $q$ range $3.8 \leq q \leq 4.6$ fm$^{-1}$ where the short-distance structure of the deuteron and non-nucleonic degrees of freedom are expected to become important. Previous measurements [3–5] of $t_{20}$ have been reported at lower momentum transfers. $F_C$ is particularly sensitive to model variations in the $q$ range $3 < q < 6$ fm$^{-1}$, where it is generally expected to pass through zero, while $F_Q$, which largely determines the cross section in this $q$ range, is less sensitive to the details of various models.

The experiment was performed at the Massachusetts Institute of Technology–Bates Linear Accelerator Center. Figure 1 shows a layout of the experimental arrangement. The electron beam from the linac was used at energies of 653, 755, and 853 (± 3) MeV, with an average current between 5 and 30 μA and a duty cycle of about 0.8%. It was incident on a 7-cm-long liquid-deuteron target. The recoil deuterons were selected in a specially designed magnetic channel, fixed at an angle of 41°, consisting of a quadrupole-quadrupole-dipole (QOD), an intermediate focus detection (IFD), and a quadrupole-quadrupole-quadrupole-dipole (QQQD) system. The scattered electrons were analyzed with a magnetic spectrometer (OHIPS), having a solid angle of 18 msr. The angle of OHIPS for each $q$ point is given in Table I. The $q$ values and their uncertainties, due to the uncertainties in the electron-beam energies and OHIPS angles (± 0.1°), are also given in Table I. The IFD was composed of two multwire proportional chambers (MWPC’s) used for tuning only and a hodoscope of ten scintillators. The “Alberta high efficiency analyzer for deuterons” (AHEAD) was installed in a shielded hut at the end of the deuteron channel. For the runs taken at the two higher electron energies, a carbon degrader was installed in front of the hodoscope. This degrader was used to reduce the flux of protons entering the polarimeter and to lower the deuteron energies to values within the maximum efficiency range of AHEAD. The coincidence between OHIPS, IFD, and AHEAD led to an unambiguous identification of $e$-$d$ elastic events.

The polarimeter was based on $d$-$p$ elastic scattering [6]. In the deuteron energy range of interest (60–170 MeV), the angular distribution of the analyzing power...
The polarization of the recoil deuterons was measured by the
polarimeter. The energies were degraded between the liquid-deuterium
target and the second dipole of the deuteron channel. The central deuteron
energies were 133 MeV for the lowest q point and 160 MeV for the two
higher q points as measured by a magnetic-field probe installed in the
second dipole of the deuteron channel.

The yield for the scattering of polarized deuterons is given by [9]

\[
N_C(\theta, \phi) = k N_0(\theta, \phi)[1 + T_{20}T_{20}(\theta) + 2T_{21}T_{21}(\theta) \cos(\phi)]
+ 2T_{22}T_{22}(\theta) \cos(2\phi)],
\]

where \(N_0\) is the yield for the scattering of unpolarized
deuterons; \(T_{20}, T_{21},\) and \(T_{22}\) are the tensor moments; \(T_{20},\)
\(T_{21},\) and \(T_{22}\) are the analyzing powers; \(\theta\) is the angle in
the center-of-mass frame between the incident and outgoing
tracks of the deuterons in the polarimeter; \(\phi\) is the angle between the
e-\(d\) and the \(d-p\) scattering planes; and \(k\) is an irrelevant
normalization factor. The yield for the scattering of unpolarized
deuterons and the analyzing powers were measured in the Saturne experiment, while
in the Bates experiment the tensor polarization of the
recoil deuterons was measured. The analyses for the cali-
bration and the Bates data proceeded in the same way.
The incident and outgoing tracks were reconstructed to
determine the scattering vertices. The \(\Delta E\) and \(E\) scintil-
lators were gain matched to identify the particles detect-
ed in the polarimeter, and the angular distribution of
detected protons was measured. A cut on the proton
missing-energy spectrum (“E-diff cut”) was applied to
the data to eliminate highly inelastic protons coming
from deuteron breakup reactions. The inclusion of some
inelastic protons resulted in analyzing powers about 20% smaller than the values quoted above. In addition,
because the deuteron energies incident on the polarimeter at
Bates had large spreads, 14–23 MeV (full width at half
maximum), and were not centered at any of the energies
in the calibration experiment, the appropriate calibration
was obtained by interpolation of the Saturne data using a
Monte Carlo technique to simulate the energy and vertex
position dependence of geometrical and absorption effects
in the polarimeter. The actual incident deuteron spatial
distributions of the Bates data were used to generate the
interpolated-calibration data, while the energy distribu-
tions, not being measured accurately, were simulated us-
ing Gaussian distributions. The final results were found
to be insensitive to reasonable changes in the above distri-
butions.

### TABLE I. Results of the \(t_{20}\) measurements.

<table>
<thead>
<tr>
<th>(q) (fm(^{-1}))</th>
<th>(\theta_r) (deg)</th>
<th>(t_{20}) ((q, \theta_r))</th>
<th>(F_C(q))</th>
<th>(F_0(q))</th>
</tr>
</thead>
<tbody>
<tr>
<td>3.78 ± 0.02</td>
<td>80.9</td>
<td>-1.24 ± 0.17(0.10)</td>
<td>0.0127 ± 0.0007</td>
<td>0.482 ± 0.116</td>
</tr>
<tr>
<td>4.22 ± 0.02</td>
<td>78.7</td>
<td>-0.82 ± 0.15(0.11)</td>
<td>0.00166 ± 0.0014</td>
<td>0.315 ± 0.016</td>
</tr>
<tr>
<td>4.62 ± 0.02</td>
<td>76.7</td>
<td>-0.41 ± 0.18(0.13)</td>
<td>-0.00147 ± 0.00013</td>
<td>0.189 ± 0.007</td>
</tr>
</tbody>
</table>
The tensor moments were obtained using a fitting procedure which adjusted the $k_q$ in Eq. (2) such that the angular distribution of the interpolated-calibration data best reproduced the relative angular distribution of the Bates data. This procedure avoids the necessity for measuring the normalization factor $k$ in the Bates experiment. The fitted values of $t_{20}$ are given in Table I. The total uncertainties given in the table combine statistical and systematic uncertainties in quadrature, while the values in parentheses indicate the systematic uncertainties only. The systematic uncertainties are due to the $E$-diff cut, differences in the calibration of the CW's between the Saturne and the Bates experiments, inexact knowledge of the deuteron energy spreads for the Bates kinematics, and the uncertainties in the interpolated-calibration data generated using the Monte Carlo simulation. In Table I, we also give the values of $F_C$ and $F_Q$ extracted from our measurements of $t_{20}$ and from a parametrization [10] of the world data for the $A$ and $B$ structure functions. The extracted $F_C$ and $F_Q$ were obtained using a standard $\chi^2$ minimization procedure. The uncertainties in $F_C$ and $F_Q$ correspond to a $\chi^2$ change from $\chi^2_{\text{min}}$ to $\chi^2_{\text{min}}+1$. A change of 1 in $\chi^2$ from its minimum value represents a 1-standard-deviation uncertainty.

The present results and previous $t_{20}$ measurements are plotted in Fig. 2. They have been adjusted using $B(F_M)$, the extracted $F_C$ and $F_Q$, and Eq. (1) to give the values for $\theta=70^\circ$, the angle at which some of the theoretical curves shown in Fig. 2 were calculated. Those calculated in the Skyrme, six-quark, and perturbative quantum chromodynamics (PQCD) models are, however, for $t_{20}$. Setting $\gamma=0$ in Eq. (1) lowers the value of $t_{20}$ around the minimum by about 0.2.

An impulse-approximation (IA) prediction calculated using conventional nonrelativistic nuclear dynamics and a representative modern potential [Argonne $V_{14}$ ($AV_{14}$) potential [11]] for the NN interaction is shown by the solid curve in Fig. 2. The addition of meson-exchange currents (MEC) results in a prediction (short-dashed curve) which clearly lies above the data for $q>3.5$ fm$^{-1}$. Other IA calculation using various realistic NN potentials (Reid soft core, Bonn, Paris) [2] show similar features. On the other hand, the $t_{20}$ prediction (double-dot-dashed curve) calculated using the new Bonn potential [12], which included an energy dependence in the potential and MEC contributions, is in good agreement with the data.

A recent relativistic one-boson-exchange prediction [13] of $t_{20}$ gives reasonable agreement with the data and is similar to the nonrelativistic IA predictions. Other relativistic calculations using the formalism of light-cone quantum mechanics [14] also give predictions for $t_{20}$ similar to those of nonrelativistic IA calculations.

Isobar degrees of freedom have been included in two coupled-channel (CC) models. In a model with very small $\Delta A$ admixtures [15], the predicted $t_{20}$ (long-dashed, curve) is in good accord with the data. The prediction of another CC model using a boundary-condition radius $r_0=0.74$ fm lies above the data (not shown in Fig. 2) and is almost indistinguishable from the prediction of the IA+MEC calculation using the $AV_{14}$ potential (short-dashed curve). Both CC models include MEC contributions, but it is noted that the $t_{20}$ prediction for the CC model with $r_0=0.74$ fm agrees with the data if the MEC contributions are removed.

The predictions of several quark-cluster models [17], calculated using the resonating-group method and a quark-bag radius of about 0.5 fm, are all in qualitative agreement with the data. One quark description excluded by the present data is a simple six-quark prediction [18] (dot-double-dashed curve), in which a six-quark component was added directly to the deuteron wave function. In this model, the node in $F_C$ is missing so that the predicted $t_{20}$ remains negative for $q>3$ fm$^{-1}$. Nonnucleonic effects are included in a totally different approach in the Skyrme model [19] where nucleons and nuclei are formed as topological solitons of pion and scalar meson fields. The value of $t_{20}$ predicted by this model (dotted curve) is in reasonable agreement with the data. Finally, the prediction of the PQCD model [20] (dot-dashed curve) clearly fails to describe the data.

The present data unambiguously show a sharp rise of $t_{20}$ from a minimum toward less negative values. This behavior is due to the node in $F_C$ which is determined using a polynomial fit at $q=4.39 \pm 0.16$ fm$^{-1}$. The extracted values of $F_C$ are plotted in Fig. 3 along with predictions for $F_C$, corresponding to the solid and short-
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FIG. 3. Extracted $|F_C|$ of the deuteron as a function of $q$. Same notations as in Fig. 2.

dashed curves in Fig. 2. As can be seen in Fig. 3, the nonrelativistic IA predictions [11] for $F_C$ of the deuteron without MEC contributions is in good agreement with the data. However, this same nonrelativistic IA model [21] requires MEC contributions to give good agreement with the data for the form factors of the three- and four-body nuclei.

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